



# *3D Numerical Analysis of the Unsteady Turbulent Swirling Flow in a Conical Diffuser using FLUENT and OpenFOAM*

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## Introduction

- Decelerated swirling flow in hydraulic turbine draft tube cone ends in **vortex breakdown** (with associated severe unsteadiness and pressure fluctuations) when operating at partial discharge.
- The main cause of VB is the **increase in swirl intensity** downstream a fixed pitch runner as the discharge decreases, as a result of the mismatch between the swirl generated by wicket gates and the angular momentum extracted by the runner.
- A certain level of **swirl at draft tube inlet avoids the flow detachment** at cone wall, and improves the conversion of the excess of kinetic energy into static pressure.
- **VB is associated with a central quasi-stagnant region**; the "vortex rope" is a rolled-up vortex sheet which originates between the central stalled region and the swirling main flow.

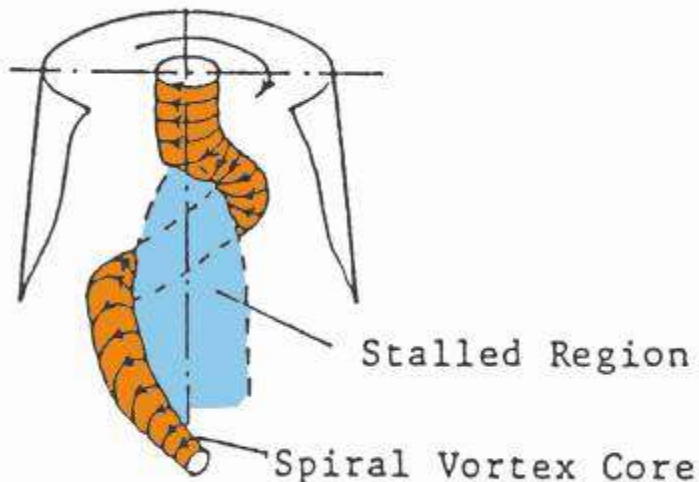




## Helical vortex breakdown in decelerated swirling flows



- The decelerated swirling flow in Francis turbine discharge cone evolves in **helical vortex breakdown** (precessing vortex rope) when the swirl number at runner outlet increases above a critical value.
- Nishi et al. (1988) suggest that the circumferentially averaged velocity field in the cone could be represented as a **"dead" (quasi-stagnant) water region surrounded by the swirling main flow**.
- The spiral vortex is a rolled-up vortex sheet originating between the central stalled region and outer swirling flow.





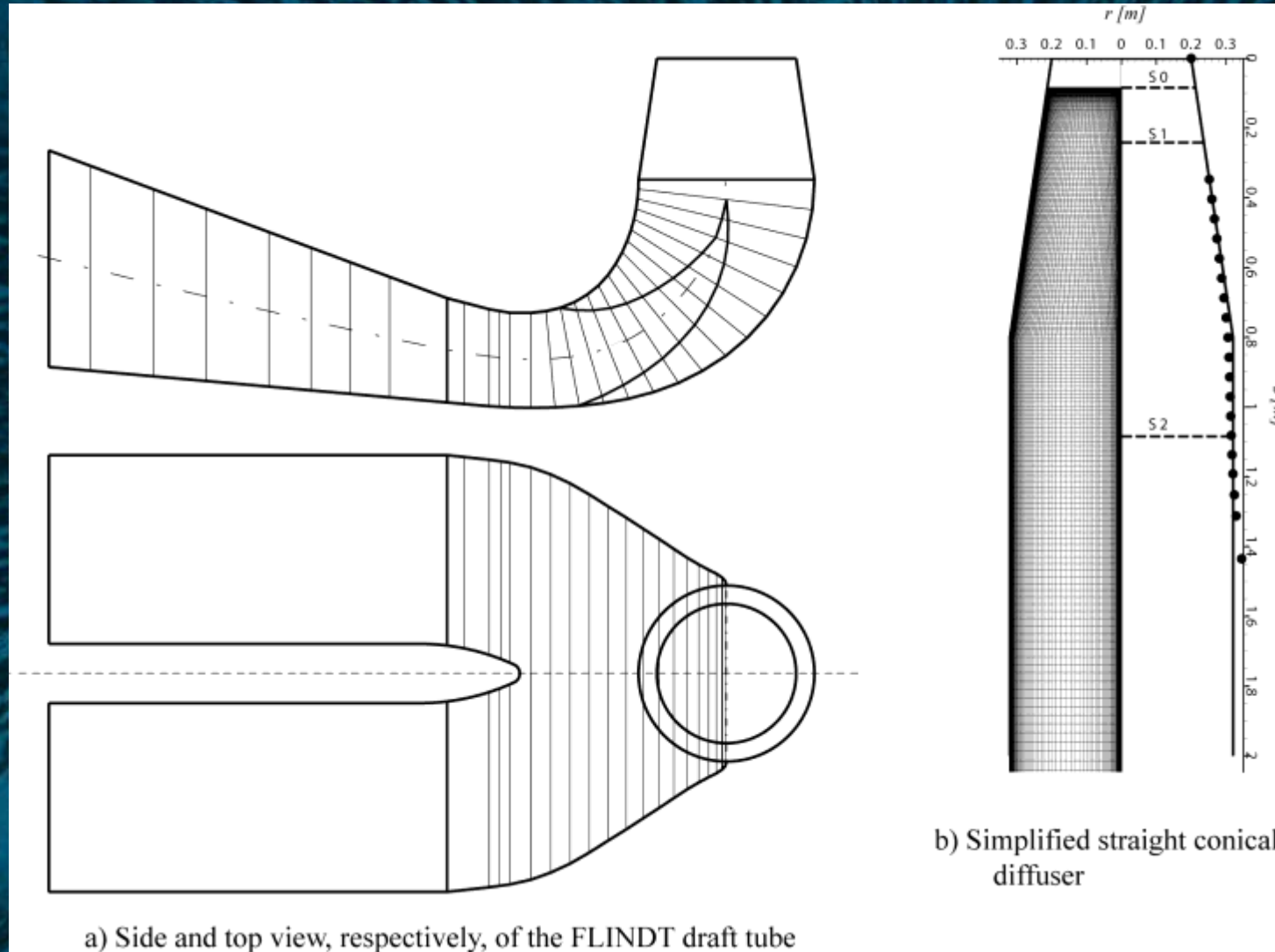
## Content

- 3D computational domain and BCs  
(computational domain corresponds to the swirling flow apparatus from test rig)
- Numerical set-up with FLUENT and OpenFOAM
- 3D unsteady turbulent flow simulation of decelerated swirl in a straight draft tube
- Vortex rope visualization
- Pressure field analysis comparison against experimental data





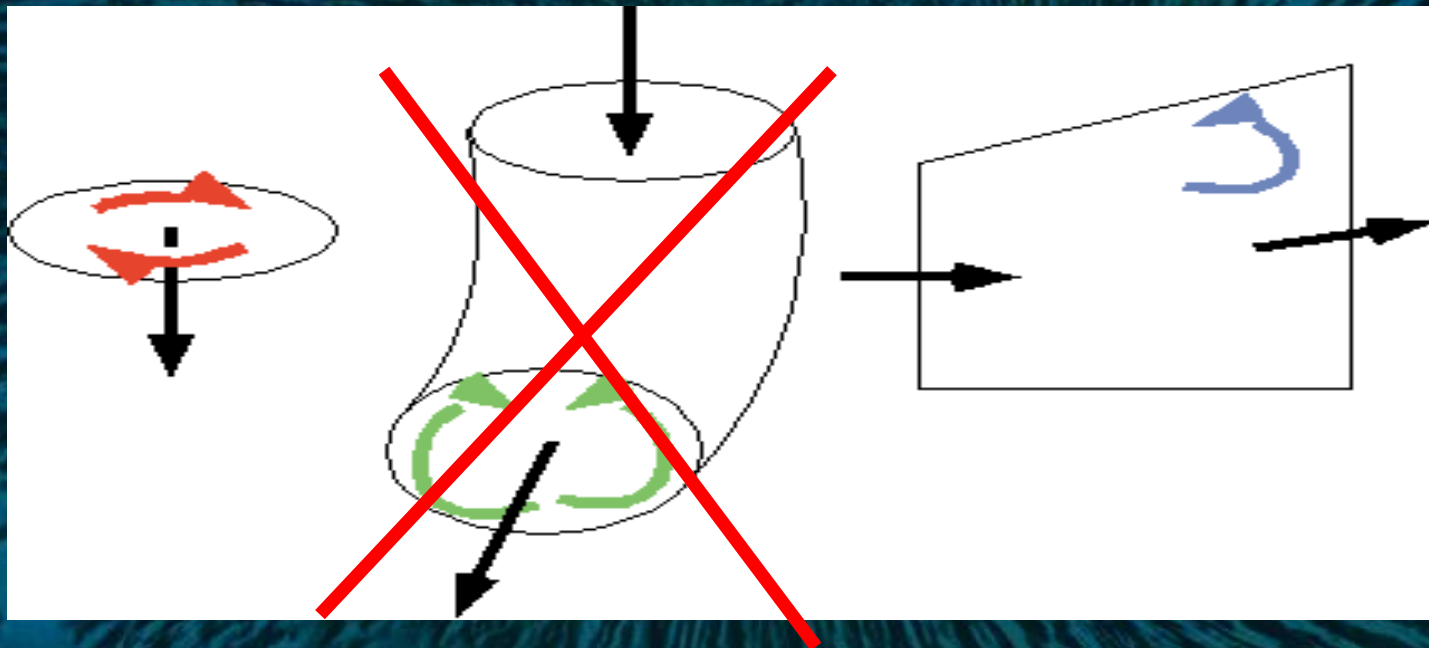
## Francis turbine draft tube and simplified straight conical diffuser





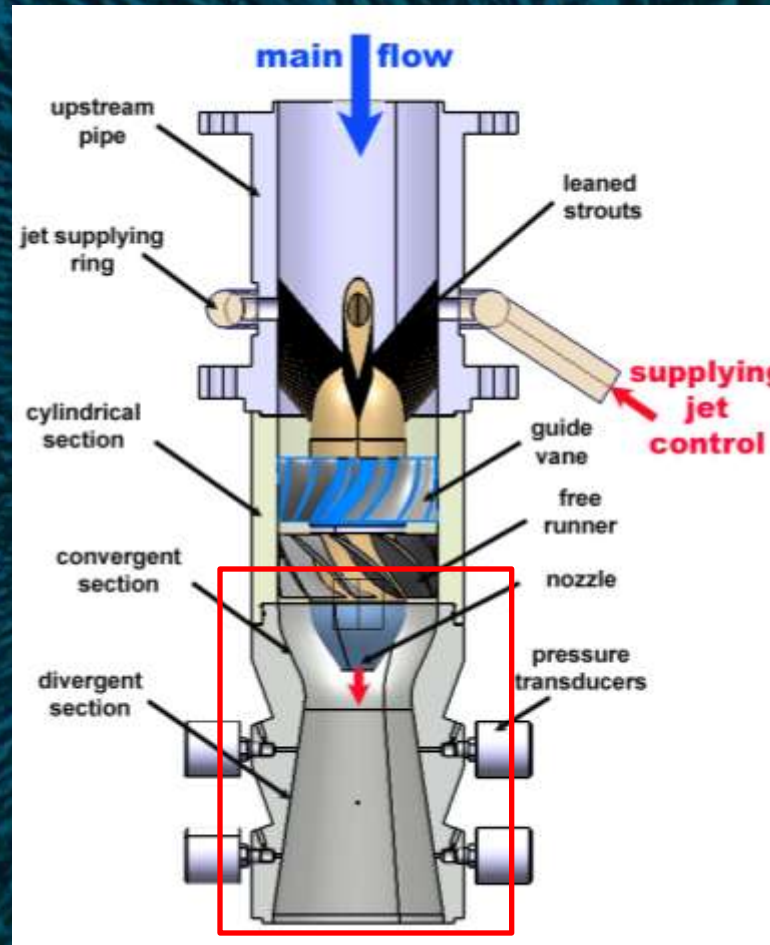
# Phenomena in the draft tube flow

- Swirling flow
- Flow into a bend – secondary flows
- Positive pressure gradient in the diffuser - separation

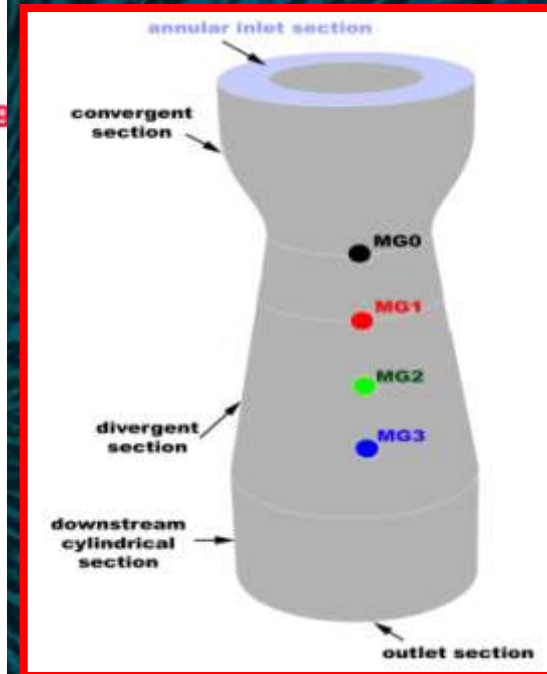




# 3D Computational domain & BCs



Meridian cross section of the  
swirling flow apparatus.



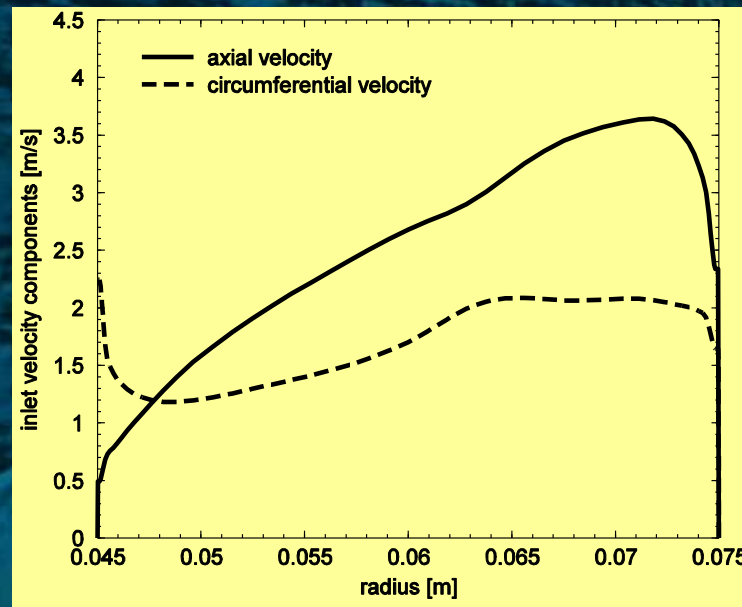
3D computational domain  
and BCs





# Boundary conditions

**Inlet** velocity profiles as computed downstream the swirl generator (fixed and rotating blades)



Axial and circumferential velocity profiles imposed on the inlet section of the 3D computational domain.



**Fluent outlet** radial equilibrium condition for pressure (relationship between pressure variation in radial direction and circumferential velocity, obtained from the radial momentum equation)

$$\frac{\partial p}{\partial r} = \frac{\rho V_{\theta}^2}{r}$$

**OpenFOAM outlet** uses zeroGradient for all variables and sets the outlet average pressure to zero.

**Wall-functions** at walls



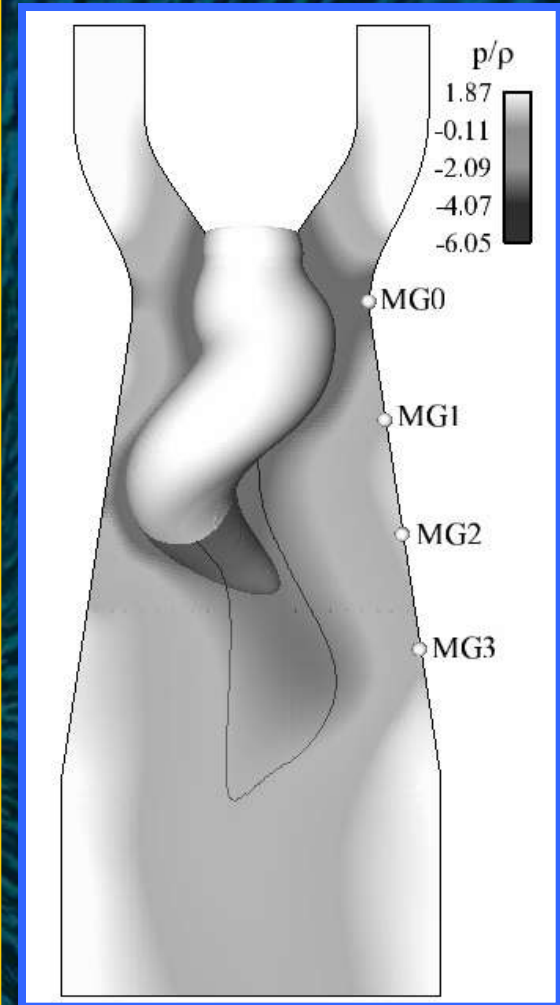
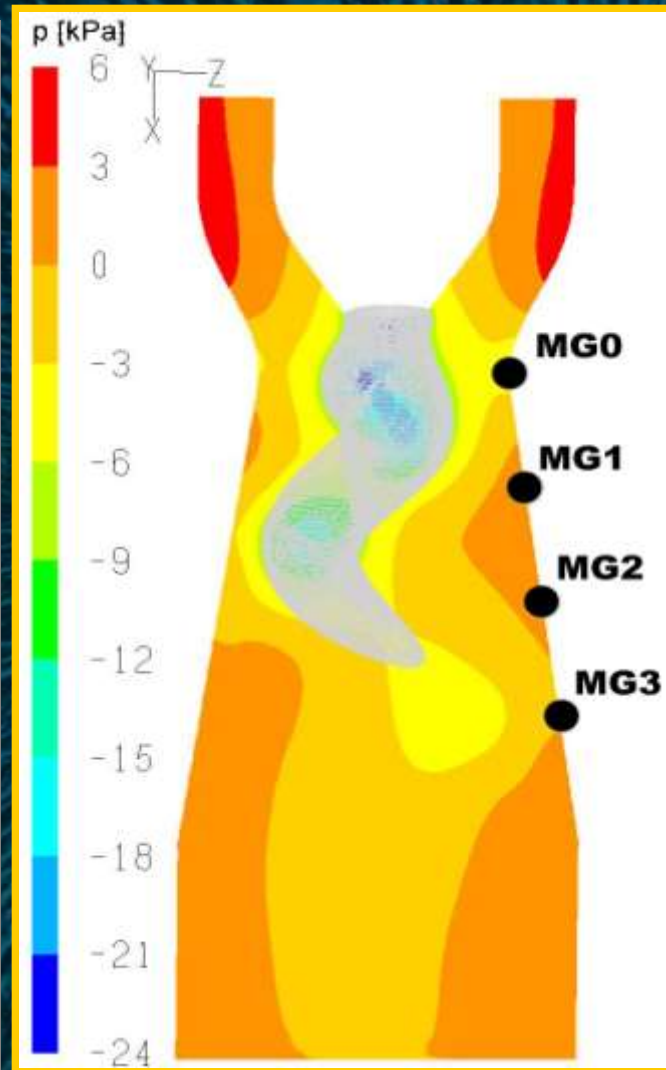
## Numerical setup

	FLUENT	OpenFOAM
Structured mesh	2 millions cells	
Velocity-pressure coupling	SIMPLE	SIMPLE
Turbulent model	k- $\epsilon$ RNG	Standard k- $\epsilon$
Pressure discretization	PRESTO	Rhie&Chow
Momentum discretization	2 <sup>nd</sup> order	2 <sup>nd</sup> order
Time discretization	1 <sup>st</sup> order	2 <sup>nd</sup> order
Time step	1e-4	5e-5





# Vortex rope visualization



St= 0.387

FLUENT 0.406 (+6%)

OpenFOAM 0.427 (10%)

3rd IAHR WorkGroup Meeting 2009, October 14-16, 2009, Brno, Czech Republic



# Fourier reconstruction on signal function

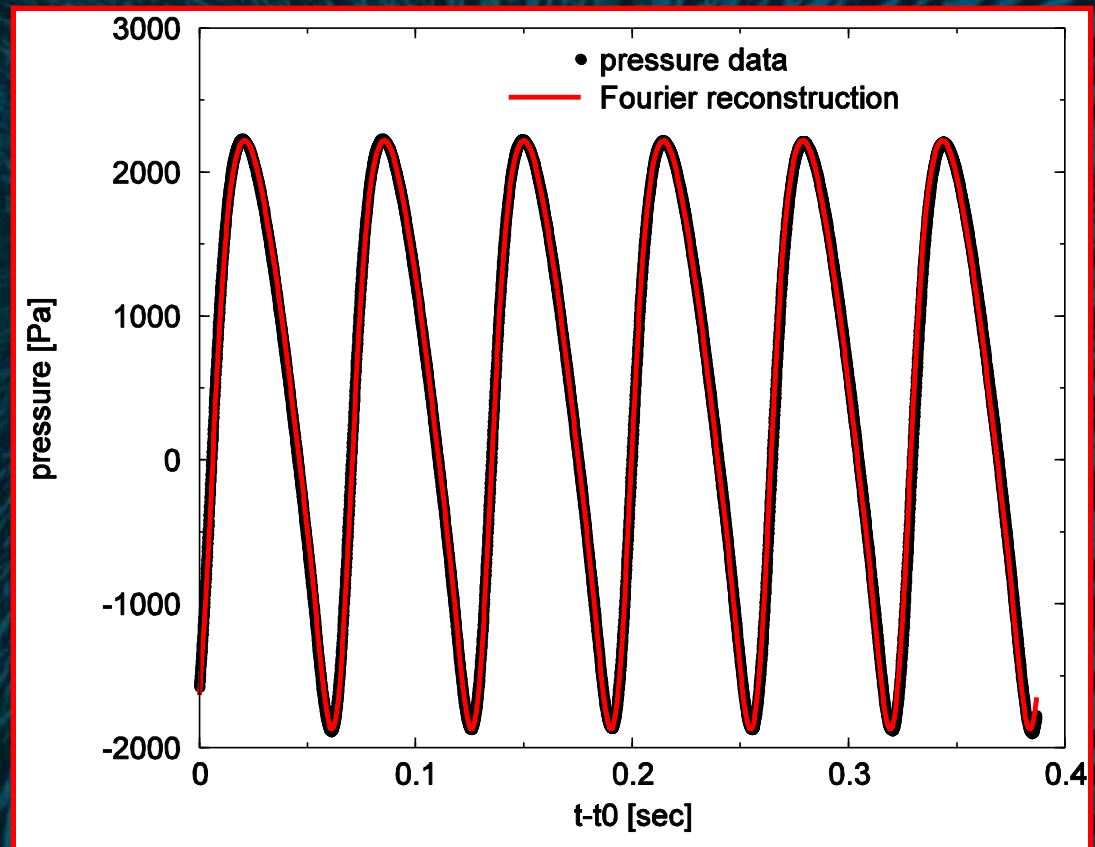
$$g(t) = A_0 + \sum_{n=1}^{(N-1)/2} A_n \cos[\omega_n(t-t_0)] - \sum_{n=1}^{(N-1)/2} B_n \sin[\omega_n(t-t_0)]$$

$$A_0 = \frac{c_0}{N} = \frac{1}{N} \sum_{n=0}^{N-1} s_n$$

$$A_n = \frac{2c_{2n}}{N}$$

$$B_n = \frac{2c_{2n+1}}{N}$$

$$\omega_n = \frac{2\pi(n+1)}{N\Delta} = \frac{2\pi(n+1)}{T}$$

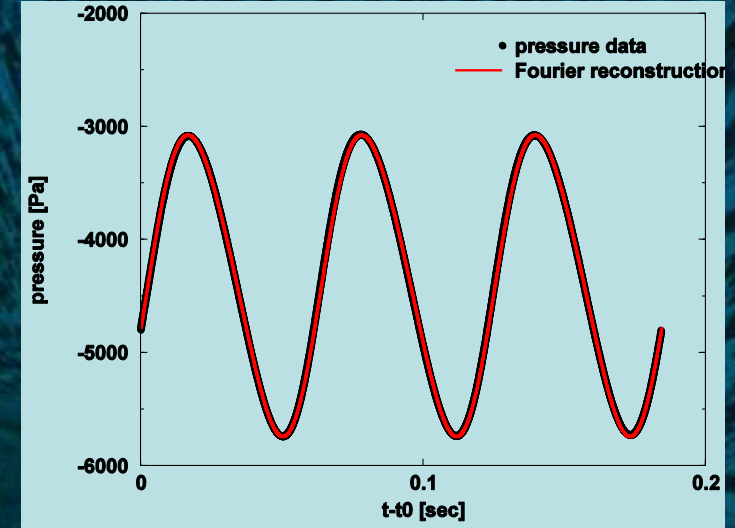
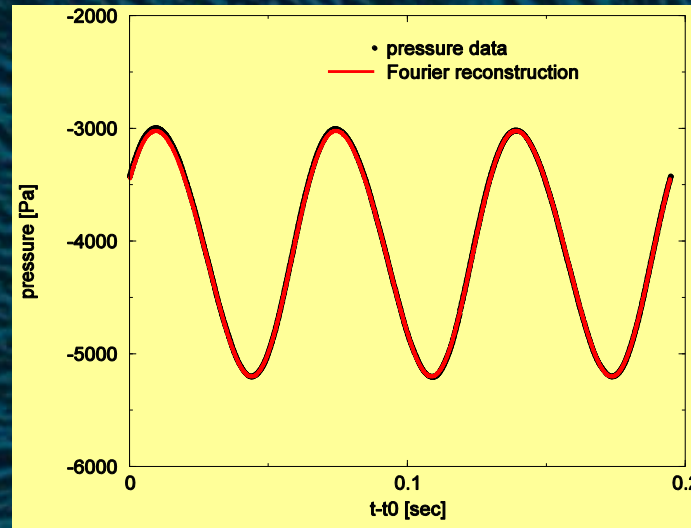




# FLUENT and OpenFOAM numerical results

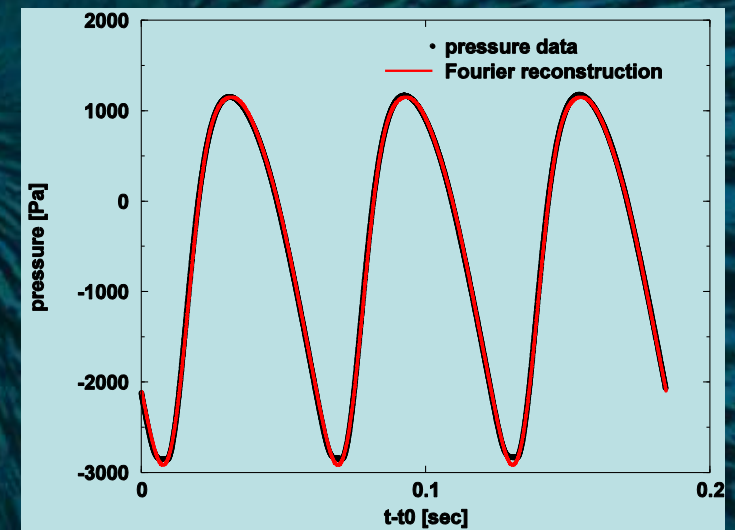
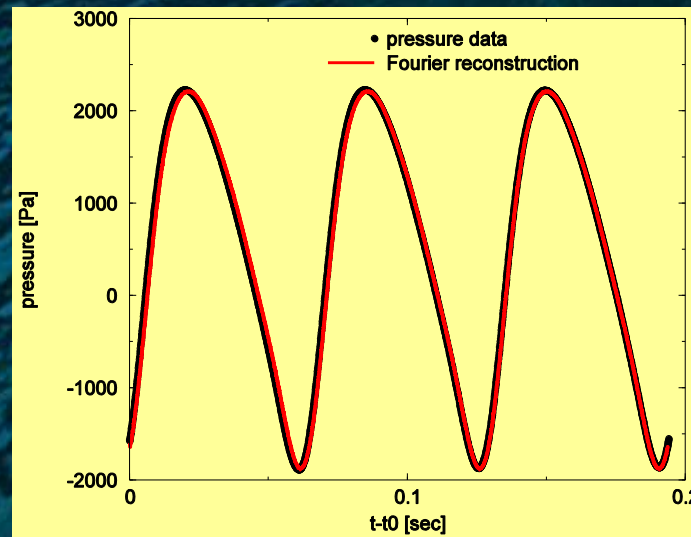
**MG0**

(base  
harmonics and  
2<sup>nd</sup> harmonics)



**MG1**

(base  
harmonics and  
higher  
harmonics up  
to 4<sup>th</sup>)

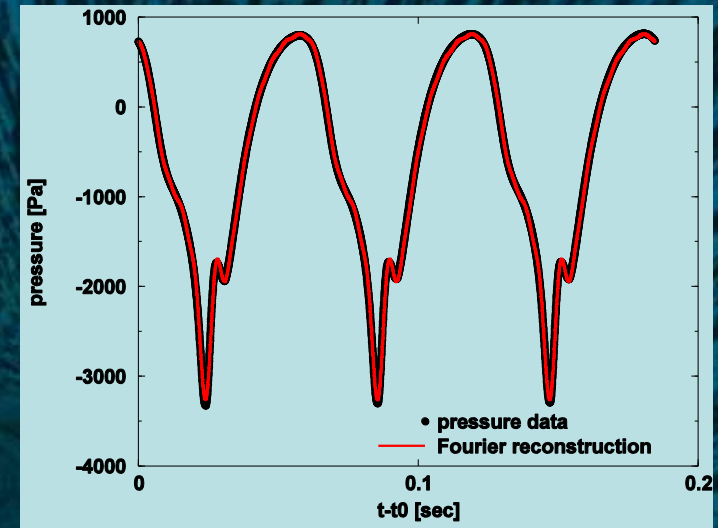
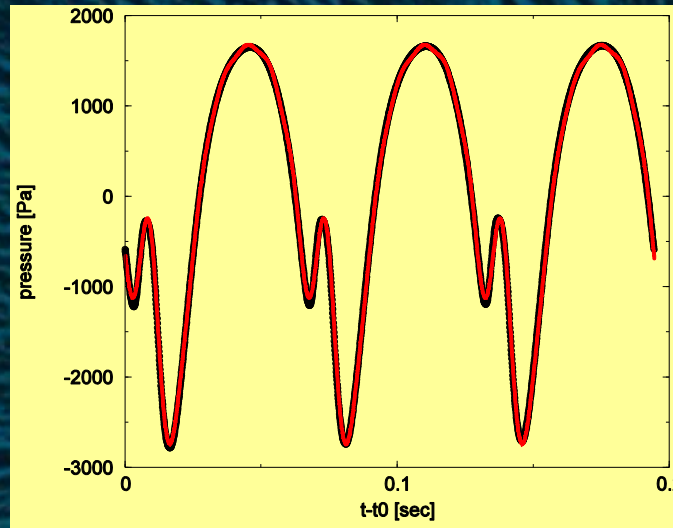




# FLUENT and OpenFOAM numerical results

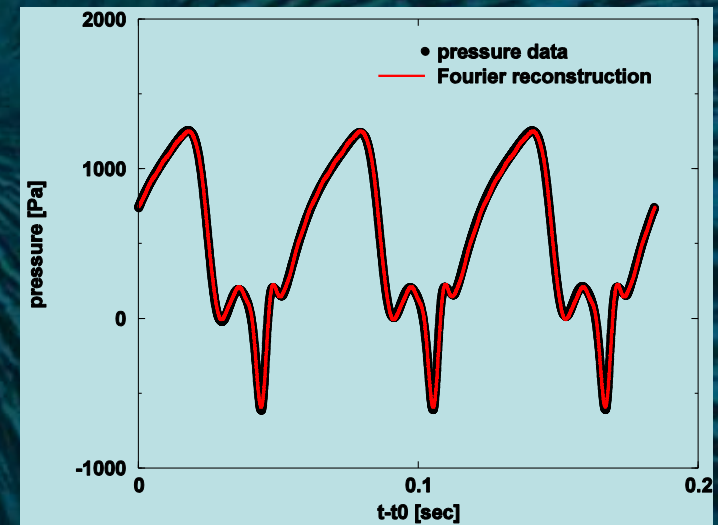
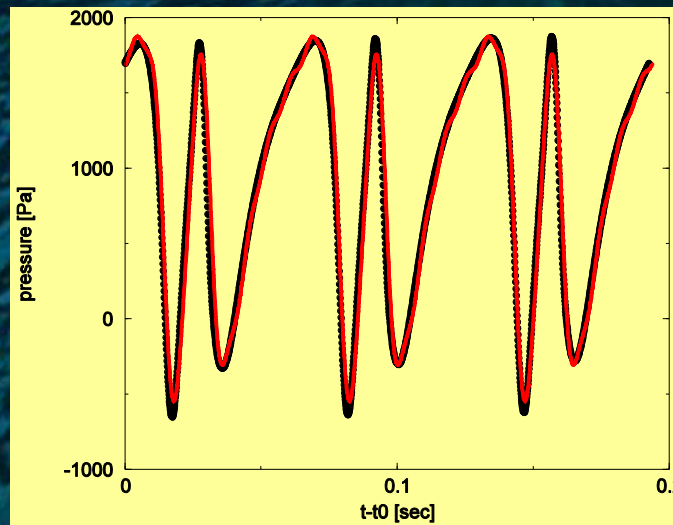
## MG2

(base harmonics  
and higher  
harmonics up to  
7<sup>th</sup>)



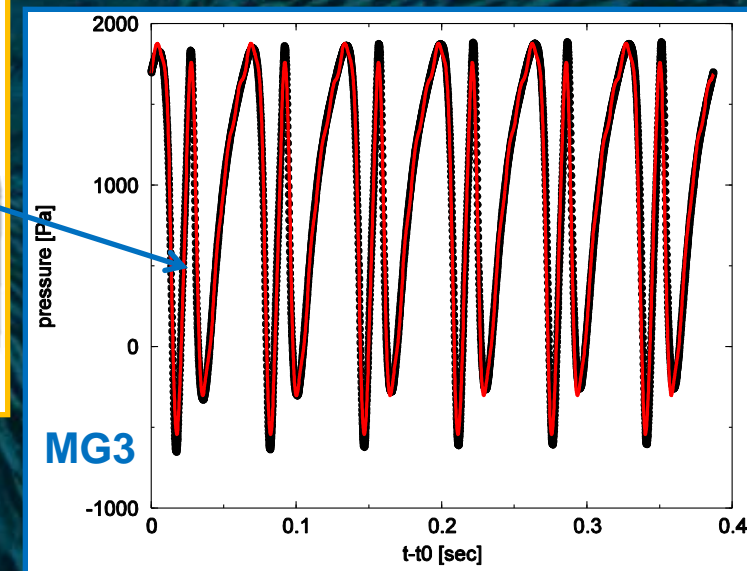
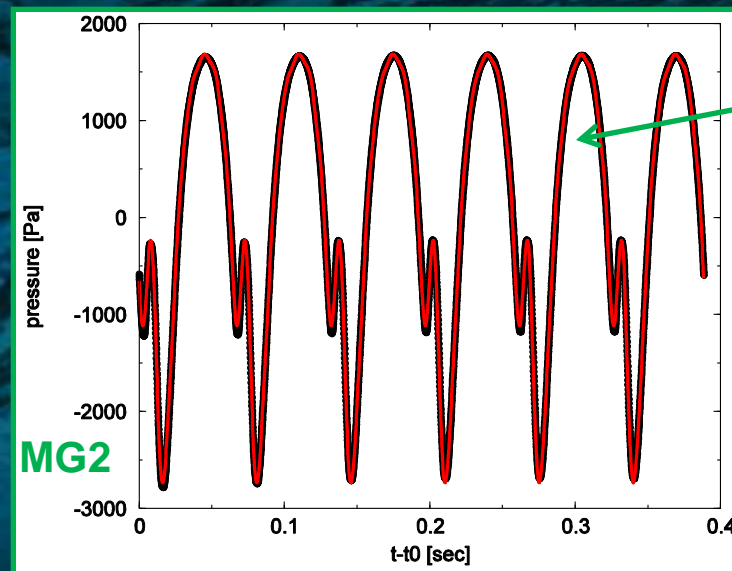
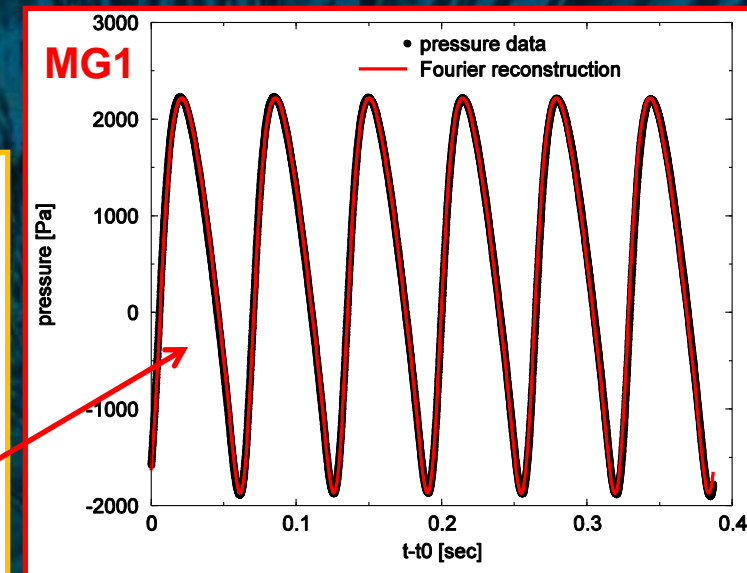
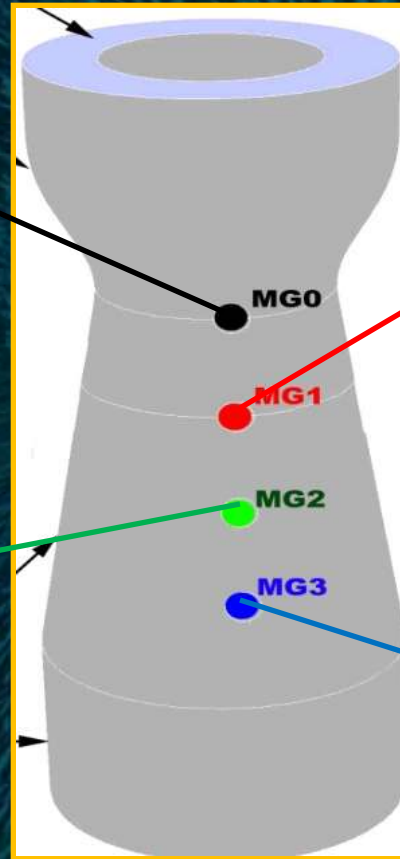
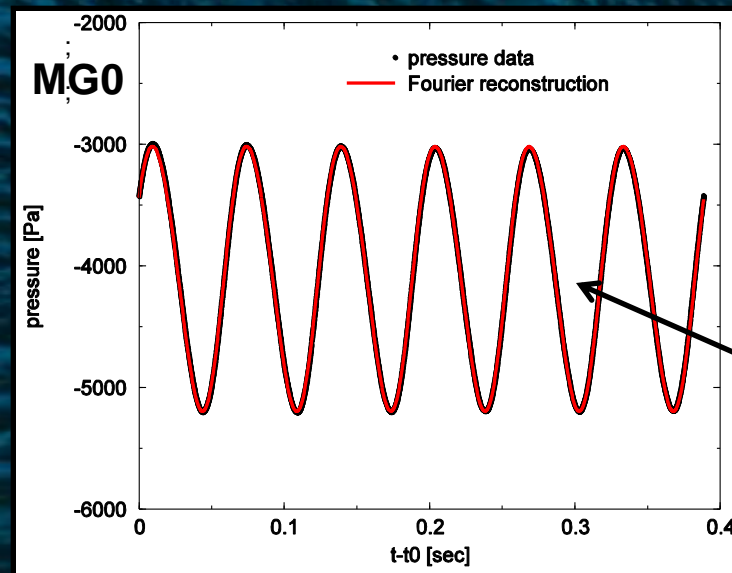
## MG3

(base harmonics  
and higher  
harmonics up to  
8<sup>th</sup>)



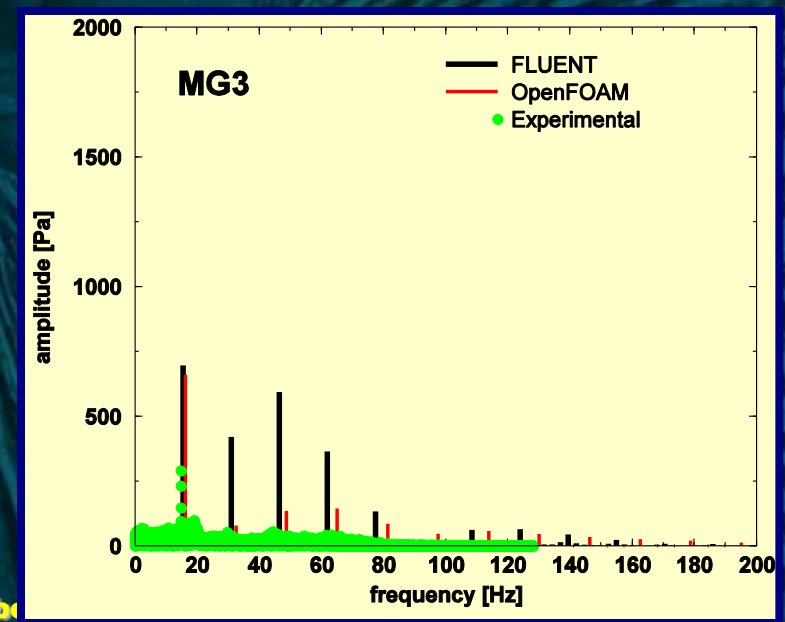
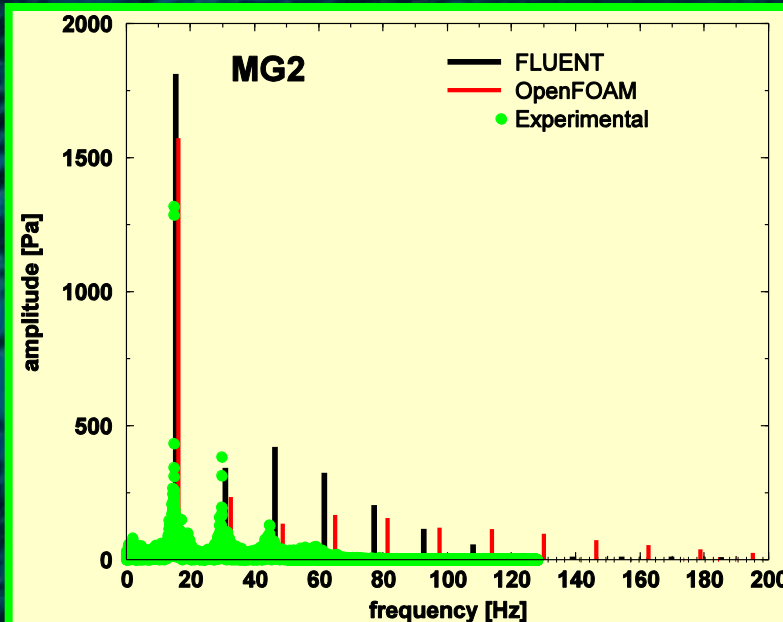
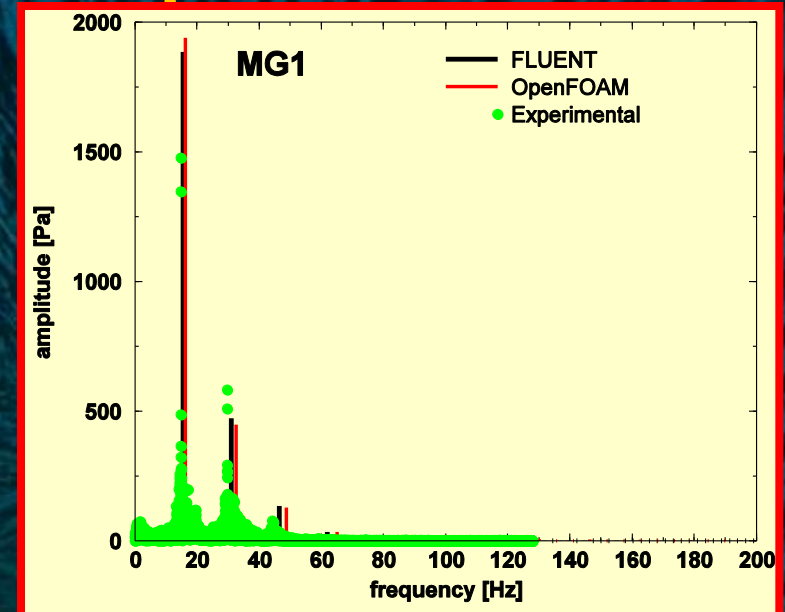
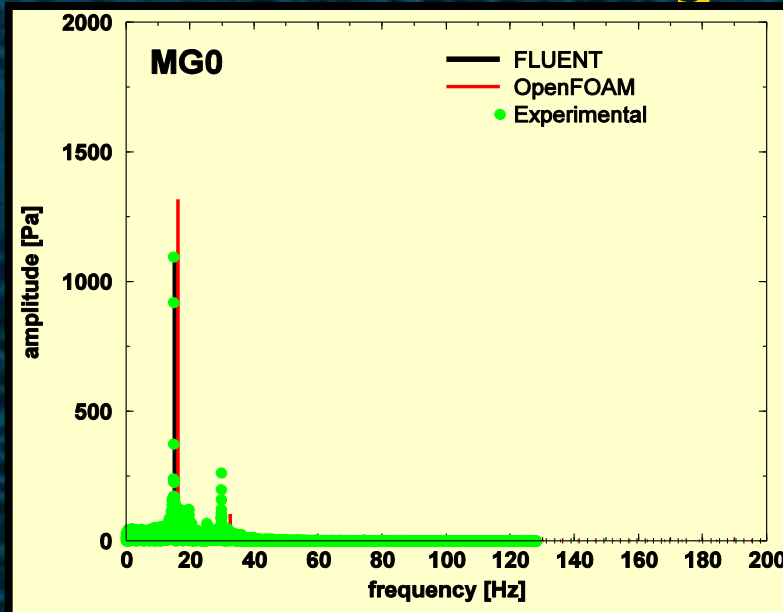


# Pressure field analysis





# Numerical results against Experimental data

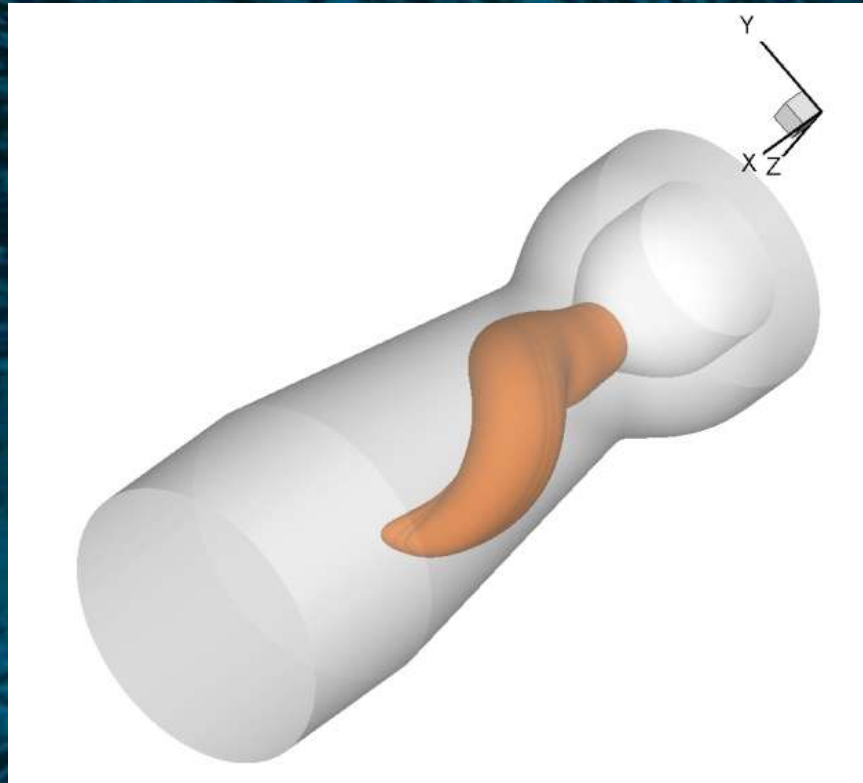




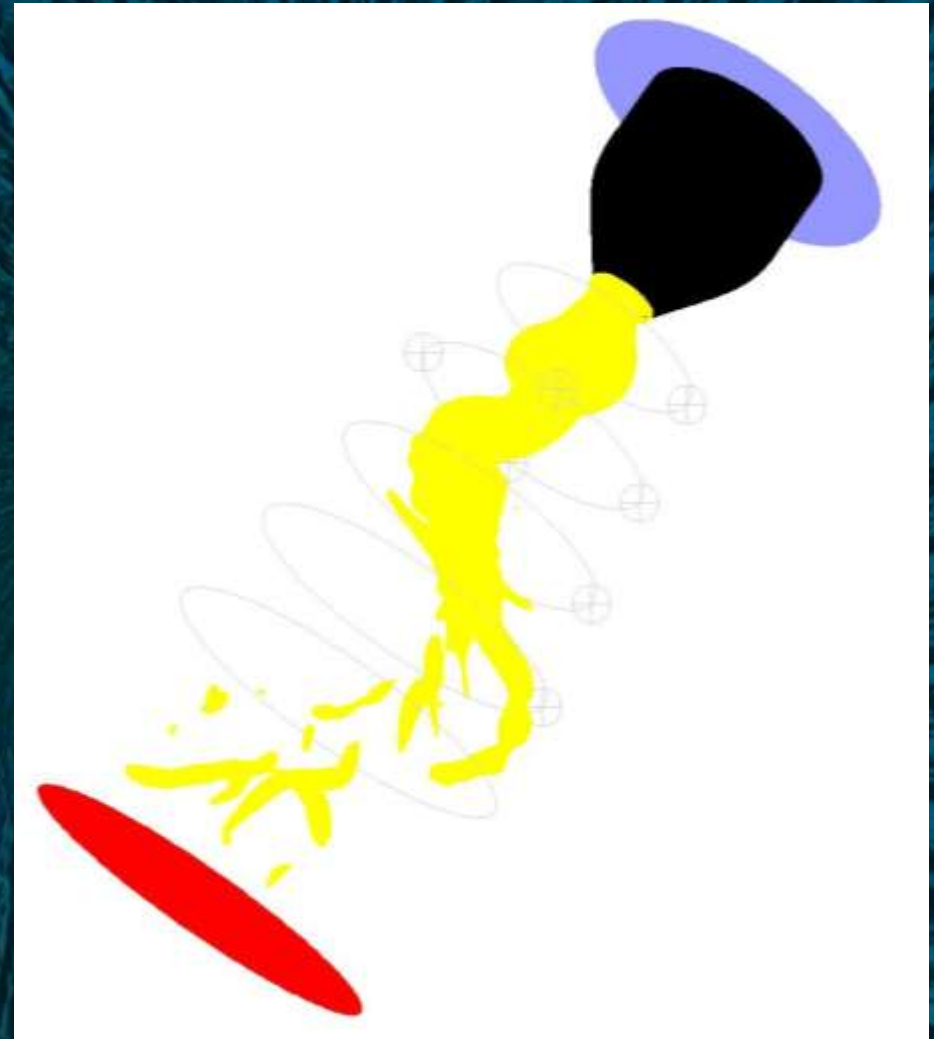
## CONCLUSIONS

- 3D unsteady turbulent ( $k$ - $\varepsilon$ ) simulations were performed using FLUENT and OpenFOAM in order to understand the physics of the decelerated swirling flow with vortex rope in conical diffuser
- The frequency is reasonably evaluated
- Pressure fluctuations associated with the vortex rope are computed in four sections of the conical diffuser → these are compared with experimental data
- The unsteady pressure field is quite well computed in the throat where the vortex rope is compact
- A significant discrepancy between numerical results and experimental data is obtained in the downstream part of the conical diffuser due to the vortex rope is too compact than the real one → improved turbulent model (DES)





vortex rope computed  
with  $k-\epsilon$  model



vortex rope computed with DES model

