

# COMPLEX MESH DEFORMATIONS IN OPENFOAM:

A CUSTOM BOUNDARY CONDITION FOR PRESCRIBED MESH MOTION

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3     introduction();           // Motivation for the work
4
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6     (
7         basics,               // dynamicMeshDict settings; boundary updates
8         laplacianMotionSolvers, // Laplace's equation, velocity and displacement solvers
9         diffusivity           // Intro to diffusivity models
10    );
11
12    timeVaryingMotionInterpolation
13    (
14        function,              // Purpose, how it works
15        compilation,           // Compilation instructions; file list
16        usage,                 // How to use
17        implementation          // How it is coded
18    );
19
20    tutorials
21    (
22        airfoil,               // A 2D deforming airfoil
23        deformingCylinder      // A 3D deforming cylinder, in parallel
24    );
25 }
```

# INTRODUCTION

OpenFOAM does not have a boundary condition for generic/arbitrary boundary motion. This is useful for experimental measurements, image registration, among others.

Example: simulations of biological flows using geometrical data from medical images.

For this purpose, a generic boundary condition for moving walls has been developed:  
`timeVaryingMotionInterpolation`

It can be used to extract motion information varying in time, from either unstructured data or regular spaced points, and interpolate this to CFD boundaries in OpenFOAM v2206.

# MESH MOTION AND DEFORMATION IN OPENFOAM

OpenFOAM has multiple tools to deal with dynamic meshes. This can be used for geometries that change in time (morphing), to deal with overset meshes, sliding meshes, moving bodies and even adaptive mesh refinement.

Dynamic meshes are mainly controlled by inputs in `dynamicMeshDict` and appropriate boundary conditions.

For mesh motion, an appropriate type of `dynamicFvMesh` is used, which in turn uses solvers and depends on boundary conditions defined for the CFD domain.

# EXAMPLE dynamicMeshDict:

Example with dynamicMotionSolverFvMesh with a single Lagrangian motion solver and an inverse distance diffusivity model based on chosen boundary or boundaries.

```
1  /*-----*-- C++ -*-----*\
2  |=====|
3  |  \ \   /   F ield      | OpenFOAM: The Open Source CFD Toolbox
4  |  \ \   /   O peration  | Version:  v2206
5  |  \ \   /   A nd        | Website:  www.openfoam.com
6  |  \ \ /   M anipulation |
7  \*-----*/
8  FoamFile
9  {
10     version      2.0;
11     format        ascii;
12     class         dictionary;
13     object        dynamicMeshDict;
14 }
15 // * * * * *
16
17 dynamicFvMesh      dynamicMotionSolverFvMesh;
18
19 motionSolverLibs    ("libfvMotionSolvers.so");
20
```

## From `dynamicMotionSolverFvMesh.C`:

```
115 bool Foam::dynamicMotionSolverFvMesh::update()
116 {
117     fvMesh::movePoints(motionPtr_->newPoints());
118
119     volVectorField* Uptr = getObjectPtr<volVectorField>("U");
120
121     if (Uptr)
122     {
123         Uptr->correctBoundaryConditions();
124     }
125
126     return true;
127 }
```

## From `motionSolver.C`:

```
200 Foam::tmp<Foam::pointField> Foam::motionSolver::newPoints()
201 {
202     solve();
203     return curPoints();
204 }
```

# LAPLACE'S EQUATION FOR MESH DEFORMATION

Calculate a mesh deformation field in the mesh.

$$\nabla \cdot (\mathbf{\Gamma}_c \nabla \mathbf{V}_c) = 0$$

Defined at cell centres!

- $\mathbf{\Gamma}_c \Rightarrow$  mesh deformation diffusivity vector
- $\mathbf{V}_c \Rightarrow$  deformation (velocities or displacements)

**Advantages:** Simple to solve, bounded, non-uniform, smooth.

**Drawback in OpenFOAM implementation:**

Requires interpolation to cell points, which can cause problems in the mesh!

# MOTION SOLVERS IN `fvMotionSolvers`:

- Velocity:
  - `velocityComponentLaplacian`
  - `velocityLaplacian`
- Displacement:
  - `displacementComponentLaplacian`
  - `displacementLaplacian`
  - `displacementSBRStress`
  - `solidBodyDisplacementLaplacian`
  - `surfaceAlignedSBRStress`



# LAPLACIAN MOTION SOLVERS IN `fvMotionSolvers`:

- `velocityComponentLaplacian` and `displacementComponentLaplacian` solve equations for one component (scalar elds).
- `velocityLaplacian` and `displacementLaplacian` solve the velocities/displacements in 3D (vector elds) and are more complete than the component version.

We will go through the two complete Lagrangian solvers to understand their function and differences. We will start with the equations they solve, moving to their implementation in OpenFOAM, focusing on their constructors, as well as the `solve()` and `curPoints()` functions.

# VELOCITY SOLVER: `velocityLaplacian`\*

- Solves Laplace's equation for a velocity field  $\mathbf{U}_c$ :

$$\nabla \cdot (\mathbf{\Gamma}_c \nabla \mathbf{U}_c) = 0$$

- Inherits from `velocityMotionSolver`` and `fvMotionSolve`.
- Interpolates data from `cellMotionU_`` and `pointMotionU_`.
- Updates point coordinates using velocity and time step:

$$\mathbf{X}_{t_n} = \mathbf{X}_{t_{n-1}} + \Delta t \cdot \mathbf{U}_p$$

\* Located at `src/fvMotionSolver/fvMotionSolvers/velocity`

# CONSTRUCTOR:

- Received references to a `polyMesh` and a `IOdictionary`.

From `velocityLaplacianFvMotionSolver.C`

```
53 Foam::velocityLaplacianFvMotionSolver::velocityLaplacianFvMotionSolver
54 (
55     const polyMesh& mesh,
56     const IOdictionary& dict
57 )
58 :
59 {}
```

# CONSTRUCTOR:

- Received references to a `polyMesh` and a `IOdictionary`.
- Initialises inheritances `velocityMotionSolver` and `fvMotionSolver`.
- Creates the `cellMotionU_`, `interpolationPtr_` and `diffusivityPtr_` objects.

From `velocityLaplacianFvMotionSolver.C`

```
57 )
58 :
59     velocityMotionSolver(mesh, dict, typeName),
60     fvMotionSolver(mesh),
61     cellMotionU_
62     (
63         IOobject
64         (
65             "cellMotionU",
66             mesh.time().timeName(),
67             mesh,
68             IOobject::READ_IF_PRESENT,
69             IOobject::AUTO_WRITE
70         ),
71         fvMesh_,
72         dimensionedVector(pointMotionU_.dimensions(), Zero),
73         cellMotionBoundaryTypes<vector>(pointMotionU_.boundaryField())
74     ),
75     interpolationPtr_
76     (
77         coeffDict().found("interpolation")
78         ? motionInterpolation::New(fvMesh_, coeffDict().lookup("interpolation"))
79         : motionInterpolation::New(fvMesh_)
80     ),
81     diffusivityPtr_
82     (
83         motionDiffusivity::New(fvMesh_, coeffDict().lookup("diffusivity"))
84     )
85 {}
```

# solve():

- movePoints doesn't do anything.
- Update diffusivity.
- updateCoeffs() is used to perform updates, as will be seen for the developed BC later on.
- fvOptions used for constrain() and correct().
- nNonOrthCorr retrieved.

From velocityLaplacianFvMotionSolver.C

```
117 void Foam::velocityLaplacianFvMotionSolver::solve()
118 {
119     // The points have moved so before interpolation update
120     // the fvMotionSolver accordingly
121     movePoints(fvMesh_.points());
122
123     diffusivityPtr_->correct();
124     pointMotionU_.boundaryFieldRef().updateCoeffs();
125
126     fv::options& fvOptions(fv::options::New(fvMesh_));
127
128     const label nNonOrthCorr
129     (
130         getDefault<label>("nNonOrthogonalCorrectors", 1)
131     );
132 }
```

# solve():

- The equation for the cell centre velocities is defined and solved.
- Non-orthogonal correctors used here but not for displacement solver. But why??

From velocityLaplacianFvMotionSolver.C

```
129     (  
130         getOrDefault<label>("nNonOrthogonalCorrectors", 1)  
131     );  
132  
133     for (label i=0; i<nNonOrthCorr; ++i)  
134     {  
135         fvVectorMatrix UEqn  
136         (  
137             fvm::laplacian  
138             (  
139                 dimensionedScalar  
140                 (  
141                     "viscosity",  
142                     dimViscosity,  
143                     1.0  
144                 )  
145                 * diffusivityPtr_-\>operator()(),  
146                 cellMotionU_,  
147                 "laplacian(diffusivity,cellMotionU)"  
148             )  
149             ==  
150             fvOptions(cellMotionU_)  
151         );  
152  
153         fvOptions.constrain(UEqn);  
154         UEqn.solveSegregatedOrCoupled(UEqn.solverDict());  
155         fvOptions.correct(cellMotionU_);  
156     }  
157 }
```

# curPoints():

- Velocities interpolated from cell centres to mesh points.
- Current points are updated using previously shown equation.

From velocityLaplacianFvMotionSolver.C

```
96 Foam::tmp<Foam::pointField>
97 Foam::velocityLaplacianFvMotionSolver::curPoints() const
98 {
99     interpolationPtr_>interpolate
100     (
101         cellMotionU_,
102         pointMotionU_
103     );
104
105     tmp<pointField> tcurPoints
106     (
107         fvMesh_.points()
108         + fvMesh_.time().deltaTValue()*pointMotionU_.primitiveField()
109     );
110
111     twoDCorrectPoints(tcurPoints.ref());
112
113     return tcurPoints;
114 }
```

# DISPL. SOLVER: `displacementLaplacian`<sup>\*</sup>

- Solves Laplace's equation for a displacement field  $\Delta \mathbf{X}_c$ :

$$\nabla \cdot (\Gamma \nabla (\Delta \mathbf{X}_c)) = 0$$

- Inherits from `displacementMotionSolver`` and `fvMotionSolver`.
- Interpolates data from `cellDisplacement_`` to `pointDisplacement_`.
- Updates points from original coordinates:

$$\mathbf{X}_{t_n} = \mathbf{X}_{t_0} + \Delta \mathbf{X}_p$$

<sup>\*</sup> Located at `src/fvMotionSolver/fvMotionSolvers/displacement/laplacian`



# CONSTRUCTOR:

- Received references to a `polyMesh` and a `IOdictionary`.

From `displacementLaplacianFvMotionSolver.C`

```
63 Foam::displacementLaplacianFvMotionSolver::displacementLaplacianFvMotionSolver
64 (
65     const polyMesh& mesh,
66     const IOdictionary& dict
67 )
68 :
69 {}
```

# CONSTRUCTOR:

- Received references to a polyMesh and a IOdictionary.
- Initialises inheritances displacementMotionSolver and fvMotionSolver.
- Creates the cellDisplacement\_, interpolationPtr\_ and diffusivityPtr\_ objects.

From displacementLaplacianFvMotionSolver.C

```
67 )
68 :
69     displacementMotionSolver(mesh, dict, typeName),
70     fvMotionSolver(mesh),
71     cellDisplacement_
72     (
73         IOobject
74         (
75             "cellDisplacement",
76             mesh.time().timeName(),
77             mesh,
78             IOobject::READ_IF_PRESENT,
79             IOobject::AUTO_WRITE
80         ),
81         fvMesh_,
82         dimensionedVector(pointDisplacement_.dimensions(), Zero),
83         cellMotionBoundaryTypes<vector>(pointDisplacement_.boundaryField())
84     ),
85     interpolationPtr_
86     (
87         coeffDict().found("interpolation")
88         ? motionInterpolation::New(fvMesh_, coeffDict().lookup("interpolation"))
89         : motionInterpolation::New(fvMesh_)
90     ),
91     diffusivityPtr_
92     (
93         motionDiffusivity::New(fvMesh_, coeffDict().lookup("diffusivity"))
94     )
95 {}
```

# CONSTRUCTOR:

- Additional tasks:
- Initialises  
pointLocation\_ and  
frozenPointsZone\_.
- pointLocation\_ used  
when applying BCs to  
points (beyond scope of this  
report).
- frozenPointsZone\_  
will not be discussed here.

From displacementLaplacianFvMotionSolver.C

```
81     fvMesh_,
82     dimensionedVector(pointDisplacement_.dimensions(), Zero),
83     cellMotionBoundaryTypes<vector>(pointDisplacement_.boundaryField())
84 ),
85 pointLocation_(nullptr),
86 interpolationPtr_
87 (
88     coeffDict().found("interpolation")
89     ? motionInterpolation::New(fvMesh_, coeffDict().lookup("interpolation"))
90     : motionInterpolation::New(fvMesh_)
91 ),
92 diffusivityPtr_
93 (
94     motionDiffusivity::New(fvMesh_, coeffDict().lookup("diffusivity"))
95 ),
96 frozenPointsZone_
97 (
98     coeffDict().found("frozenPointsZone")
99     ? fvMesh_.pointZones().findZoneID
100     (
101         coeffDict().get<word>("frozenPointsZone")
102     )
103     : -1
104 )
105 {
106     IOobject io
107     (
108         "pointLocation",
109         fvMesh_.time().timeName(),
```

# CONSTRUCTOR:

- Additional tasks:
- Initialises  
pointLocation\_ and  
frozenPointsZone\_.
- pointLocation\_ used  
when applying BCs to  
points (beyond scope of this  
report).
- frozenPointsZone\_  
will not be discussed here.

From displacementLaplacianFvMotionSolver.C

```
99      ? fvMesh_.pointZones().findZoneID
100      (
101          coeffDict().get<word>("frozenPointsZone")
102      )
103      : -1
104  )
105  {
106      IOobject io
107      (
108          "pointLocation",
109          fvMesh_.time().timeName(),
110          fvMesh_,
111          IOobject::MUST_READ,
112          IOobject::AUTO_WRITE
113      );
114
115      if (debug)
116      {
117          Info<< "displacementLaplacianFvMotionSolver:" << nl
118              << "    diffusivity          : " << diffusivityPtr_.type() << nl
119              << "    frozenPoints zone : " << frozenPointsZone_ << endl;
120      }
121
122
123      if (io.typeHeaderOk<pointVectorField>(true))
124      {
125          pointLocation_.reset
126          (
127              new pointVectorField
```

# CONSTRUCTOR:

- Additional tasks:
- Initialises  
pointLocation\_ and  
frozenPointsZone\_.
- pointLocation\_ used  
when applying BCs to  
points (beyond scope of this  
report).
- frozenPointsZone\_  
will not be discussed here.

From displacementLaplacianFvMotionSolver.C

```
117         Info<< "displacementLaplacianFvMotionSolver:" << nl
118             << "         diffusivity          : " << diffusivityPtr_.type() << nl
119             << "         frozenPoints zone : " << frozenPointsZone_ << endl;
120     }
121
122
123     if (io.typeHeaderOk<pointVectorField>(true))
124     {
125         pointLocation_.reset
126         (
127             new pointVectorField
128             (
129                 io,
130                 pointMesh::New(fvMesh_)
131             )
132         );
133
134         if (debug)
135         {
136             Info<< "displacementLaplacianFvMotionSolver : "
137                 << " Read pointVectorField "
138                 << io.name()
139                 << " to be used for boundary conditions on points."
140                 << nl
141                 << "Boundary conditions:"
142                 << pointLocation_.boundaryField().types() << endl;
143         }
144     }
145 }
```

# solve():

- movePoints doesn't do anything.
- Update diffusivity.
- updateCoeffs() is used to perform updates, as will be seen for the developed BC later on.
- fvOptions used for constrain() and correct().

From displacementLaplacianFvMotionSolver.C

```
327 void Foam::displacementLaplacianFvMotionSolver::solve()
328 {
329     // The points have moved so before interpolation update
330     // the motionSolver accordingly
331     movePoints(fvMesh_.points());
332
333     diffusivity().correct();
334     pointDisplacement_.boundaryFieldRef().updateCoeffs();
335
336     fv::options& fvOptions(fv::options::New(fvMesh_));
337
338     // We explicitly do NOT want to interpolate the motion inbetween
339     // different regions so bypass all the matrix manipulation.
340     fvVectorMatrix TEqn
341     (
342         fvm::laplacian
343         (
344             dimensionedScalar("viscosity", dimViscosity, 1.0)
345             *diffusivity().operator>(),
346             cellDisplacement_,
347             "laplacian(diffusivity,cellDisplacement)"
348         )
349     ==
350     fvOptions(cellDisplacement_)
351 );
352
353 fvOptions.constrain(TEqn);
354 TEqn.solveSegregatedOrCoupled(TEqn.solverDict());
355 fvOptions.correct(cellDisplacement_);
```

# solve():

- The equation for the cell centre velocities is defined and solved.
- This solver does not use non-orthogonal correctors. But why??

From displacementLaplacianFvMotionSolver.C

```
329 // The points have moved so before interpolation update
330 // the motionSolver accordingly
331 movePoints(fvMesh_.points());
332
333 diffusivity().correct();
334 pointDisplacement_.boundaryFieldRef().updateCoeffs();
335
336 fv::options& fvOptions(fv::options::New(fvMesh_));
337
338 // We explicitly do NOT want to interpolate the motion inbetween
339 // different regions so bypass all the matrix manipulation.
340 fvVectorMatrix TEqn
341 (
342     fvm::laplacian
343     (
344         dimensionedScalar("viscosity", dimViscosity, 1.0)
345         *diffusivity().operator>(),
346         cellDisplacement_,
347         "laplacian(diffusivity,cellDisplacement)"
348     )
349     ==
350     fvOptions(cellDisplacement_)
351 );
352
353 fvOptions.constrain(TEqn);
354 TEqn.solveSegregatedOrCoupled(TEqn.solverDict());
355 fvOptions.correct(cellDisplacement_);
356 }
```



# curPoints():

- Displacements interpolated from cell centres to mesh points.
- Current points are updated using previously shown equation.

From displacementLaplacianFvMotionSolver.C

```
261 Foam::tmp<Foam::pointField>
262 Foam::displacementLaplacianFvMotionSolver::curPoints() const
263 {
264     interpolationPtr_>interpolate
265     (
266         cellDisplacement_,
267         pointDisplacement_
268     );
269
270     if (pointLocation_)
271     {
272         if (debug)
273         {
274             Info<< "displacementLaplacianFvMotionSolver : applying
275                 << " boundary conditions on " << pointLocation_().n
276                 << " to new point location."
277                 << endl;
278         }
279
280         pointLocation_().primitiveFieldRef() =
281             points0()
282             + pointDisplacement_.primitiveField();
283
284         pointLocation_().correctBoundaryConditions();
285
286         // Implement frozen points
287         if (frozenPointsZone_ != -1)
288         {
289             const pointZone& pz = fvMesh_.pointZones()[frozenPoints
```



# curPoints():

- Displacements interpolated from cell centres to mesh points.
- Current points are updated using previously shown equation.

From displacementLaplacianFvMotionSolver.C

```
296
297     twoDCorrectPoints(pointLocation_.primitiveFieldRef());
298
299     return tmp<pointField>(pointLocation_.primitiveField());
300 }
301 else
302 {
303     tmp<pointField> tcurPoints
304     (
305         points0() + pointDisplacement_.primitiveField()
306     );
307     pointField& curPoints = tcurPoints.ref();
308
309     // Implement frozen points
310     if (frozenPointsZone_ != -1)
311     {
312         const pointZone& pz = fvMesh_.pointZones()[frozenPoints
313
314         forAll(pz, i)
315         {
316             curPoints[pz[i]] = points0()[pz[i]];
317         }
318     }
319
320     twoDCorrectPoints(curPoints);
321
322     return tcurPoints;
323 }
324 }
```

# DIFFUSIVITY MODELS:

Available in folder `src/fvMotionSolver/motionDiffusivity/`.

- `uniformDiffusivity`
- `inverseDistance`
- `inverseFaceDistance`
- `inversePointDistance`
- `inverseVolume`
- `directional`
- `motionDirectional`
- `file`

# DIFFUSIVITY MODELS:

- Very poor descriptions in source files.
- Available models may be modified with a **square** or an **exponential** function.
- Selecting an appropriate model:

## VERY IMPORTANT! MODEL SPECIFIC!

- Inverse distance methods tend to outperform uniform models <sup>[1]</sup> <sup>[2]</sup>

[1] H. Jasak and Z. Tukovic, "Automatic mesh motion for the unstructured finite volume method", Transactions of FAMENA, vol. 30, no. 2, pp. 1--20, 2006.

[2] R. Löhner and C. Yang, "Improved ALE mesh velocities for moving bodies", Communications in Numerical Methods in Engineering, vol. 12, no. 10, pp. 599--608, 1996.

# `timeVaryingMotionInterpolation:`

Developed for seamless integration with `fvMotionSolvers`.

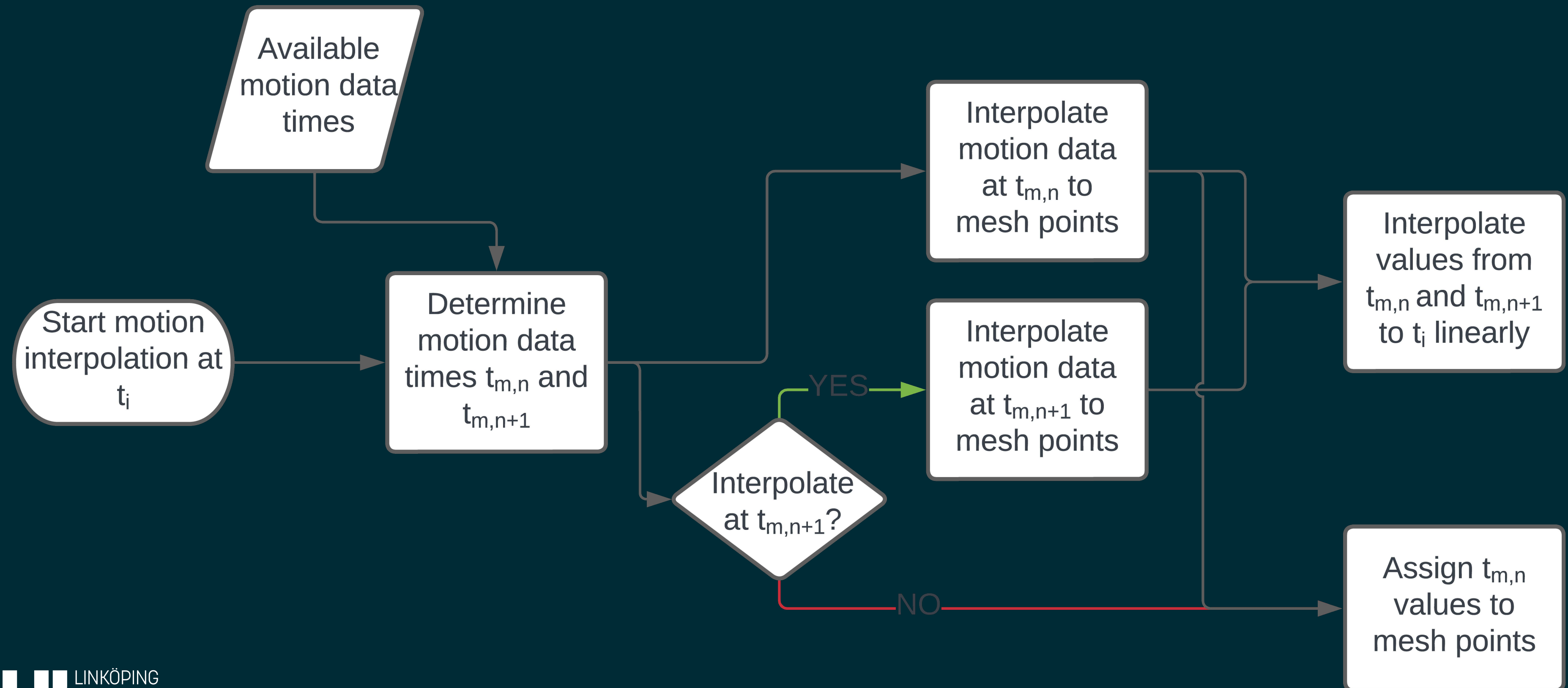
Compiled as part of a new library names `myFvMotionSolvers`, which can be used in `dynamicMeshDict`.

Allows arbitrary motion information to be applied to boundaries.

Motion/deformation may be obtained experimentally, from image registration, etc.

We'll go through it in steps!

# FLOWCHART FOR timeVaryingMotionInterpolation:



# INPUTS TO timeVaryingMotionInterpolation:

Field	Default	Accepted values
inputType	unstructured	unstructured, structured
interpolationType	nearest	nearest, inverseDist, trilinear
inverseDistRadius	-	Any float value
inputFolderName	Boundary name.	A folder name
intOutsideBounds	true	true, false
value	-	Any value of the field type

# COMPILATION OF timeVaryingMotionInterpolation:

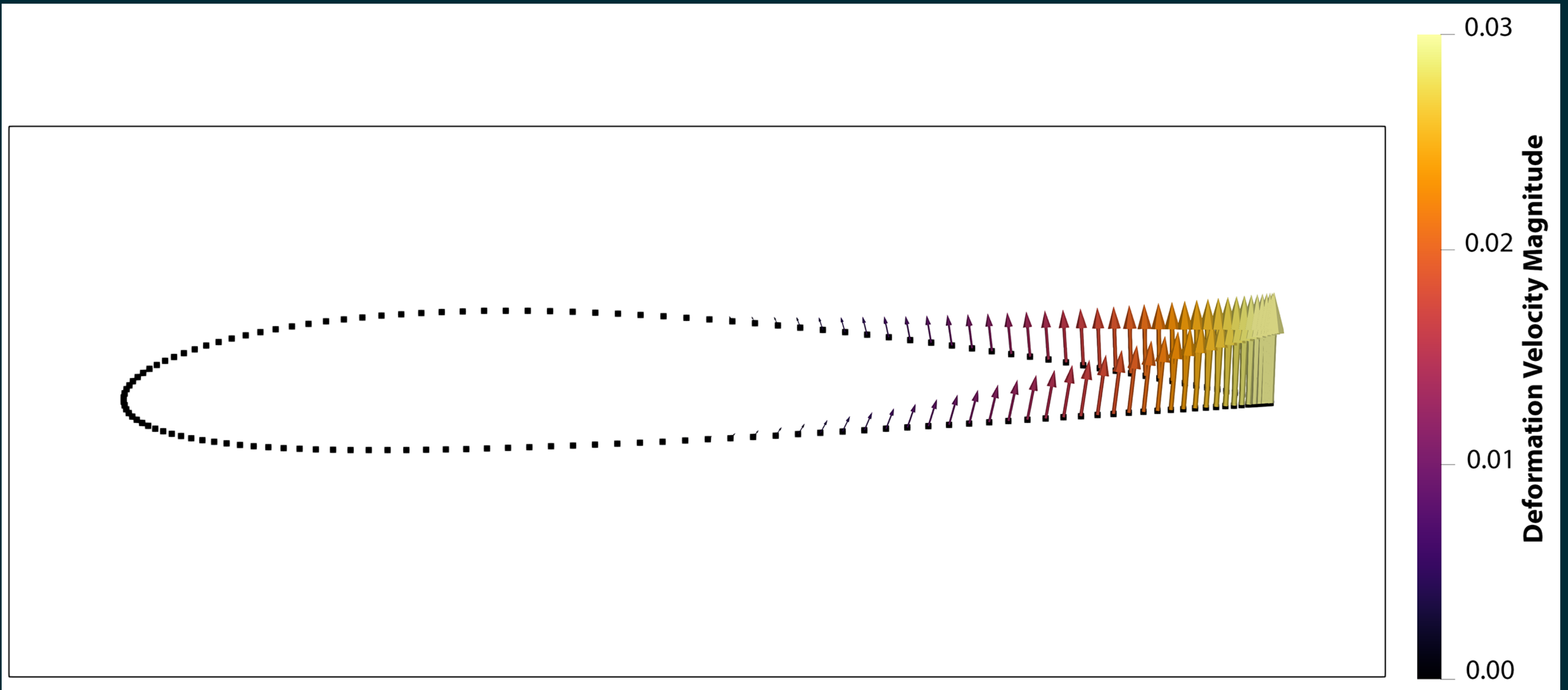
Provided files:

```
1 myFvMotionSolver
2 |-- Allwclean
3 |-- Allwmake
4 |-- Make
5 |   |-- files
6 |   |-- options
7 |-- pointPatchFields
8     |-- derived
9       |-- timeVaryingMotionInterpolation
10         |-- timeVaryingMotionInterpolationPointPatchField.C
11         |-- timeVaryingMotionInterpolationPointPatchField.H
12         |-- timeVaryingMotionInterpolationPointPatchFields.C
13         |-- timeVaryingMotionInterpolationPointPatchFields.H
```

Compilation either using wmake or the provided script Allwmake.

Add **motionSolverLibs** ("myFvMotionSolvers.so"); to dynamicMeshDict.

# EXAMPLE OF UNSTRUCTURED MOTION DATA:





# UNSTRUCTURED MOTION DATA INPUTS:

Files for point coordinates and motion (velocity or displacement).

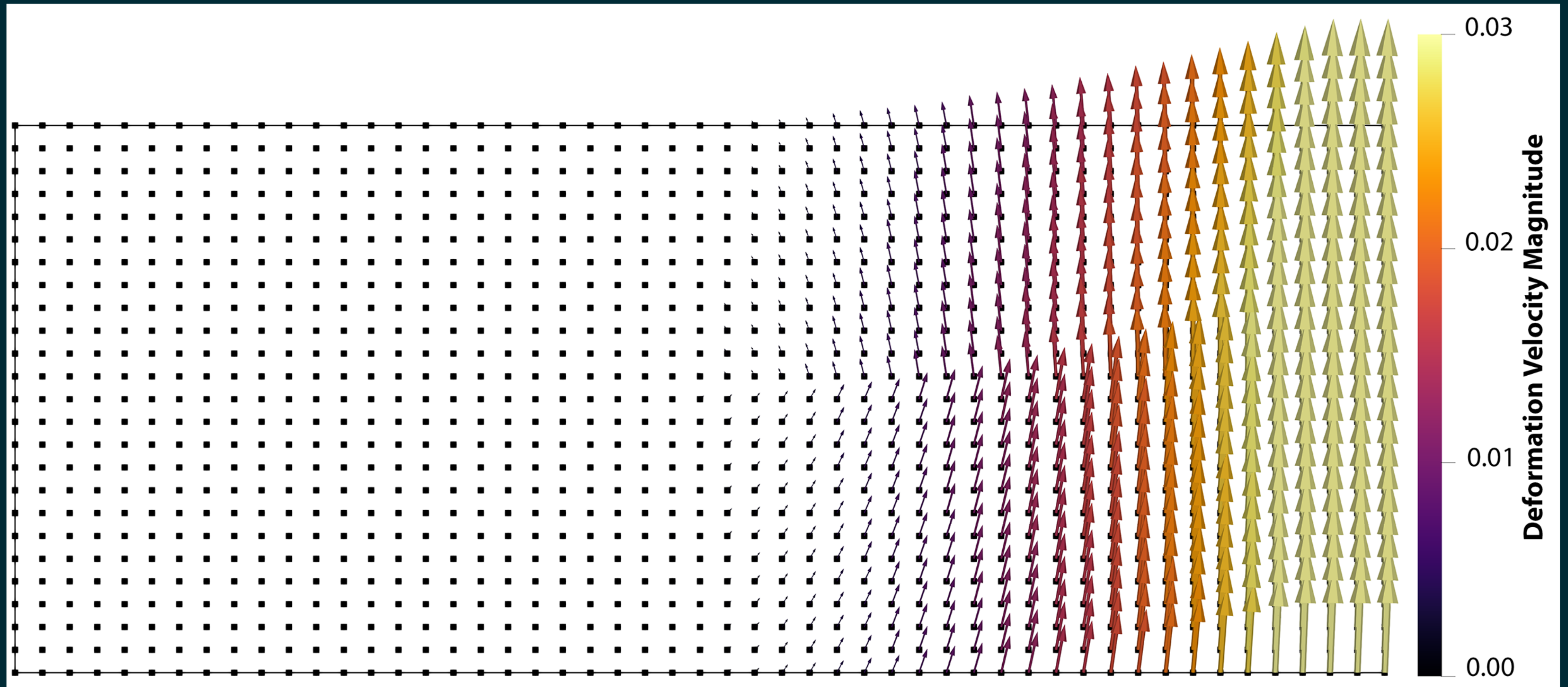
```
1 // Example points file
2 N
3 (
4 (pX_0      pY_0      pZ_0      )
5 (pX_1      pY_1      pZ_1      )
6 (pX_2      pY_2      pZ_2      )
7
8 ...
9
10 (pX_N-1    pY_N-1    pZ_N-1    )
11 )
```

```
1 // Example motion data file
2 N
3 (
4 (mX_0      mY_0      mZ_0      )
5 (mX_1      mY_1      mZ_1      )
6 (mX_2      mY_2      mZ_2      )
7
8 ...
9
10 (mX_N-1    mY_N-1    mZ_N-1    )
11 )
```

```
1 `-- inputFolderName
2   |-- 0.0000
3   |   |-- pointDisplacement
4   |   |-- points
5   |-- 0.0500
6   |   |-- pointDisplacement
7   ...
8   |-- 9.9500
9   |   |-- pointDisplacement
10  |   |-- points
```

Example folder structure.

# EXAMPLE OF STRUCTURED MOTION DATA:



# STRUCTURED MOTION DATA INPUTS:

Motion data files (velocity or displacement) and matrix information file.

```
1 // Example domainMatrixInfo file
2 // Motion data matrix information.
3 // Line 1: reference point      (x,y,z).
4 // Line 2: voxels sizing       (dx,dy,dz).
5 // Line 3: matrix dimensions   (nx,ny,nz).
6 3
7 (
8 (x_ref  y_ref  z_ref )
9 (d_x    d_y    d_z   )
10 (N_x    N_y    N_z   )
11 )
```

```
1 // Example motion data file
2 N
3 (
4 (mX_0      mY_0      mZ_0      )
5 (mX_1      mY_1      mZ_1      )
6 (mX_2      mY_2      mZ_2      )
7
8 ...
9
10 (mX_N-1    mY_N-1    mZ_N-1    )
11 )
```

```
1 `-- inputFolderName
2   |-- 0.0000
3   |-- `-- pointMotionU
4   |-- 0.0500
5   |-- `-- pointMotionU
6   ...
7   |-- 9.9500
8   |-- `-- pointMotionU
9   `-- domainMatrixInfo
```

Example folder structure.

# STRUCTURED MATRIX FORMAT:

For a point with indices  $i_{x,p}$ ,  $i_{y,p}$  and  $i_{z,p}$ , its coordinates are

$$x_p = x_{\text{ref}} + i_{x,p}(\Delta x)$$

$$y_p = y_{\text{ref}} + i_{y,p}(\Delta y)$$

$$z_p = z_{\text{ref}} + i_{z,p}(\Delta z) .$$

```
1 // Example domainMatrixInfo file
2 // Motion data matrix information.
3 // Line 1: reference point      (x,y,z).
4 // Line 2: voxels sizing       (dx,dy,dz).
5 // Line 3: matrix dimensions   (nx,ny,nz).
6 3
7 (
8  x_ref  y_ref  z_ref )
9  d_x    d_y    d_z   )
10 (N_x    N_y    N_z   )
11 )
```

OpenFOAM reads data as a list, so an index  $m_p$  is needed:

$$m_p = i_{x,p} + i_{y,p}(N_x) + i_{z,p}(N_x \cdot N_y)$$

# PRIVATE VARIABLES:

From `timeVaryingMotionInterpolationPointPatchField.H`

```
57 template<class Type>
58 class timeVaryingMotionInterpolationPointPatchField
59 :
60     public fixedValuePointPatchField<Type>
61 {
62     // Private data
63
64     //- Name of the field data table, defaults to the name of the field
65     word fieldName_;
66
67     //- List of boundaryData time directories
68     instantList sampleTimes_;
69
70     //- Current starting index in sampleTimes
71     label startSampleTime_;
72
73     //- Interpolated values from startSampleTime
74     Field<Type> startSampledValues_;
75
76     //- Current end index in sampleTimes
77     label endSampleTime_;
78
79     //- Interpolated values from endSampleTime
80     Field<Type> endSampledValues_;
81
```

# PRIVATE VARIABLES:

From timeVaryingMotionInterpolationPointPatchField.H

```
81
82     //- Input data type
83     word inputType_;
84
85     //- Interpolation type
86     word interpolationType_;
87
88     //- Custom boundary subfolder
89     word inputFolderName_;
90
91     //- Use custom boundary folder?
92     Switch useCustomFolder_;
93
94     //- Outside bounds action
95     Switch intOutsideBounds_;
96
97     //- Inverse distance search radius
98     scalar inverseDistRadius_;
99
100    //- Sample data coordinates at start
101    pointField startSamplePoints_;
102
103    //- Sample data values at start
104    Field<Type> startSampleData_;
105
```



# PRIVATE VARIABLES:

From timeVaryingMotionInterpolationPointPatchField.H

```
95         Switch intOutsideBounds_;
96
97         //- Inverse distance search radius
98         scalar inverseDistRadius_;
99
100        //- Sample data coordinates at start
101        pointField startSamplePoints_;
102
103        //- Sample data values at start
104        Field<Type> startSampleData_;
105
106        //- Sample data coordinates at end
107        pointField endSamplePoints_;
108
109        //- Sample data values at end
110        Field<Type> endSampleData_;
111
112        //- Reference point for sample data coordinates
113        vector domainRefPt_;
114
115        //- Dimensions (number of voxels in x, y, z) from sample data
116        vector domainMatDm_;
117
118        //- Voxel sizing for sample data voxels (x, y, z)
119        vector domainVoxSz_;
```

# updateCoeffs()

From timeVaryingMotionInterpolationPointPatchField.C

```
1379 template<class Type> 57
1380 void Foam::timeVaryingMotionInterpolationPointPatchField<Type>::updateCoeffs()
1381 {
1382     if (this->updated())
1383     {
1384         return;           // Check if already updated
1385     }
1386
1387     checkTable();         // Call checkTable() function
1388
1389     // Interpolate between the sampled data
1390     scalar deltaTime = this->db().time().value() - sampleTimes_[startSampleTime_].value();
1391     if (endSampleTime_ == -1 || deltaTime < SMALL)
1392     {
1393         // only start value
1394         if (debug)
1395         {
1396             Pout<< "updateCoeffs : Sampled, non-interpolated values"
1397                 << " from start time:"
1398                 << sampleTimes_[startSampleTime_].name() << nl;
1399         }
1400
1401         this->operator==(startSampledValues_); // Assign startSampledValues_
1402     }
1403     else
```



# updateCoeffs()

From timeVaryingMotionInterpolationPointPatchField.C

```
1383     {
1384         return;           // Check if already updated
1385     }
1386
1387     checkTable();         // Call checkTable() function
1388
1389     // Interpolate between the sampled data
1390     scalar deltaTime = this->db().time().value() - sampleTimes_[startSampleTime_].value();
1391     if (endSampleTime_ == -1 || deltaTime < SMALL)
1392     {
1393         // only start value
1394         if (debug)
1395         {
1396             Pout<< "updateCoeffs : Sampled, non-interpolated values"
1397                 << " from start time:"
1398                 << sampleTimes_[startSampleTime_].name() << nl;
1399         }
1400
1401         this->operator==(startSampledValues_); // Assign startSampledValues_
1402     }
1403     else
1404     {
1405         scalar start = sampleTimes_[startSampleTime_].value(); // t_{m,n}
1406         scalar end = sampleTimes_[endSampleTime_].value();     // t_{m,n+1}
1407
1408         scalar s = (this->db().time().value() - start) / (end - start); // Linear interp. factor
```

# updateCoeffs()

From timeVaryingMotionInterpolationPointPatchField.C

```
1399     }
1400
1401     this->operator==(startSampledValues_); // Assign startSampledValues_
1402 }
1403 else
1404 {
1405     scalar start = sampleTimes_[startSampleTime_].value(); // t_{m,n}
1406     scalar end = sampleTimes_[endSampleTime_].value(); // t_{m,n+1}
1407
1408     scalar s = (this->db().time().value()-start)/(end-start); // Linear interp. factor
1409
1410     if (debug)
1411     {
1412         Pout<< "updateCoeffs : Sampled, interpolated values"
1413             << " between start time:"
1414             << sampleTimes_[startSampleTime_].name()
1415             << " and end time:" << sampleTimes_[endSampleTime_].name()
1416             << " with weight:" << s << endl;
1417     }
1418     this->operator==((1-s)*startSampledValues_ + s*endSampledValues_); // Interpolate in time
1419 }
1420
1421
1422 if (debug)
1423 {
```

# updateCoeffs()

From timeVaryingMotionInterpolationPointPatchField.C

```
1406         scalar end = sampleTimes_[endSampleTime_].value();           // t_{m,n+1}
1407
1408         scalar s = (this->db().time().value()-start)/(end-start);      // Linear interp. factor
1409
1410         if (debug)
1411         {
1412             Pout<< "updateCoeffs : Sampled, interpolated values"
1413                 << " between start time:"
1414                 << sampleTimes_[startSampleTime_].name()
1415                 << " and end time:" << sampleTimes_[endSampleTime_].name()
1416                 << " with weight:" << s << endl;
1417         }
1418         this->operator==( (1-s)*startSampledValues_ + s*endSampledValues_); // Interpolate in time
1419     }
1420
1421
1422     if (debug)
1423     {
1424         Pout<< "updateCoeffs : set fixedValue to min:" << gMin(*this)
1425             << " max:" << gMax(*this)
1426             << " avg:" << gAverage(*this) << endl;
1427     }
1428
1429     fixedValuePointPatchField<Type>::updateCoeffs(); // Run updateCoeffs() from parent class
1430 }
```

# checkTable()

From timeVaryingMotionInterpolationPointPatchField.C

```
322 template<class Type>
323 void Foam::timeVaryingMotionInterpolationPointPatchField<Type>::checkTable()
324 {
325     const Time& time = this->db().time();           // Reference to time
326
327     const polyMesh& pMesh = this->patch().boundaryMesh().mesh(); // Reference to boundary mesh
328
329     // Read the initial point position
330     pointField meshPts;                             // Point coordinates
331
332     if (pMesh.pointsInstance() == pMesh.facesInstance())
333     {
334         meshPts = pointField(pMesh.points(), this->patch().meshPoints());
335     }
336     else
337     {
338         // Load points from facesInstance
339         if (debug)
340         {
341             Info<< "Reloading points0 from " << pMesh.facesInstance()
342                 << endl;
343         }
344
345         pointIOField points0
346         (
```

# checkTable()

From timeVaryingMotionInterpolationPointPatchField.C

```
335     }
336     else
337     {
338         // Load points from facesInstance
339         if (debug)
340         {
341             Info<< "Reloading points0 from " << pMesh.facesInstance()
342                 << endl;
343         }
344
345         pointIOField points0
346         (
347             IOobject
348             (
349                 "points",
350                 pMesh.facesInstance(),
351                 polyMesh::meshSubDir,
352                 pMesh,
353                 IOobject::MUST_READ,
354                 IOobject::NO_WRITE,
355                 false
356             )
357         );
358         meshPts = pointField(points0, this->patch().meshPoints());
359     }
360
```

# checkTable()

From timeVaryingMotionInterpolationPointPatchField.C

```
357         );
358         meshPts = pointField(points0, this->patch().meshPoints());
359     }
360
361     // Initialise
362     if (startSampleTime_ == -1 && endSampleTime_ == -1)
363     {
364         // Structured domain properties file path
365         // (Defined here because it's path is used anyways)
366         const fileName domainInfoFile
367         (
368             time.path()
369             /time.caseConstant()
370             /"boundaryData"
371             /inputFolderName_
372             /"domainMatrixInfo"
373         );
374
375         // Read the times for which data is available
376
377         const fileName samplePointsDir = domainInfoFile.path();
378         sampleTimes_ = Time::findTimes(samplePointsDir);           // Find available times
379
380         if (debug)
381         {
382             Info<< "timeVaryingMotionInterpolationPointPatchField : In directory "
```

# checkTable()

From timeVaryingMotionInterpolationPointPatchField.C

```
387
388     // Read structured data domain properties
389     if (inputType_ == "structured")
390     {
391         IOobject ioDomainInfoFile                // Read the domain information
392         (
393             domainInfoFile,    // absolute path
394             time,
395             IOobject::MUST_READ,
396             IOobject::NO_WRITE,
397             false,              // no need to register
398             true                // is global object (currently not used)
399         );
400         const rawIOField<point> domainInformationData(ioDomainInfoFile, false);
401         if (domainInformationData.size() != 3 && domainInformationData.size() != 6)
402         {
403             FatalErrorInFunction
404             << "Length of file 'domainMatrixInfo' (" << domainInformationData.size()
405             << ") differs from allowed values (3 and 6) in file "
406             << domainInfoFile << exit(FatalError);
407         }
408         domainRefPt_ = domainInformationData[0];    // Reference point
409         domainVoxSz_ = domainInformationData[1];    // Matrix spacing
410         domainMatDm_ = domainInformationData[2];    // Matrix dimensions
411         // Create a variable with the structured point coordinates
412         // THIS IS NOT EFFICIENT, BUT SHOULD NOT BE FORBIDDEN!!!
```

# checkTable()

From timeVaryingMotionInterpolationPointPatchField.C

```
413         if (interpolationType_ != "trilinear")
414         {
415             int m;
416             int matSize = domainMatDm_.x()*domainMatDm_.y()*domainMatDm_.z();
417             tmp<pointField> tstrPts(new pointField(matSize));
418             pointField& strPts = tstrPts.ref();
419             for(int ii = 0; ii<domainMatDm_.x(); ii++)
420             {
421                 for(int jj = 0; jj<domainMatDm_.y(); jj++)
422                 {
423                     for(int kk = 0; kk<domainMatDm_.z(); kk++)
424                     {
425                         m = (kk)*(domainMatDm_.x()*domainMatDm_.y()) +
426                             (jj)*(domainMatDm_.x()) +
427                             (ii);
428                         strPts[m] = point
429                         (
430                             domainRefPt_.x()+ii*domainVoxSz_.x(),
431                             domainRefPt_.y()+jj*domainVoxSz_.y(),
432                             domainRefPt_.z()+kk*domainVoxSz_.z()
433                         );
434                     }
435                 }
436             }
437             startSamplePoints_ = tstrPts;    // Calculate a matrix with all structured points
```



# checkTable()

From timeVaryingMotionInterpolationPointPatchField.C

```
435         }
436     }
437     startSamplePoints_ = tstrPts;    // Calculate a matrix with all structured points
438 }
439 }
440 }
441
442 // Find current time in sampleTimes
443 label lo = -1;
444 label hi = -1;
445
446 bool foundTime = pointToPointPlanarInterpolation::findTime // Find indices of time folders
447 (
448     sampleTimes_,
449     startSampleTime_,
450     time.value(),
451     lo,                // Index for t_{m,n}
452     hi                 // Index for t_{m,n+1}
453 );
454
455 if (!foundTime)
456 {
457     FatalErrorInFunction
458     << "Cannot find starting sampling values for current time "
459     << time.value() << nl
460     << "Have sampling values for times "
```

# checkTable()

From timeVaryingMotionInterpolationPointPatchField.C

```
468
469
470 // Update START sampled data fields.
471 if (lo != startSampleTime_)
472 {
473     startSampleTime_ = lo;
474
475     if (startSampleTime_ == endSampleTime_)
476     {
477         // No need to reread since are end values
478         if (debug)
479         {
480             Pout<< "checkTable : Setting startValues to (already read) "
481                 << "boundaryData"
482                 << "/inputFolderName_"
483                 << "/sampleTimes_[startSampleTime_].name()"
484                 << endl;
485         }
486         startSampleData_ = endSampleData_; // Previous t_{m,n+1} for t_{m,n}
487         if (inputType_ == "unstructured")
488         {
489             startSamplePoints_ = endSamplePoints_;
490         }
491     }
492 else
493 {
```

# checkTable()

From timeVaryingMotionInterpolationPointPatchField.C

```
500         << endl;
501     }
502
503     // Reread field values at points
504     const fileName valsFile
505     (
506         time.path()
507         /time.caseConstant()
508         /"boundaryData"
509         /inputFolderName_
510         /sampleTimes_[startSampleTime_].name()
511         /fieldName_
512     );
513     IOobject ioField
514     (
515         valsFile,           // absolute path
516         time,
517         IOobject::MUST_READ,
518         IOobject::NO_WRITE,
519         false,             // no need to register
520         true               // is global object (currently not used)
521     );
522     startSampleData_ = rawIOField<Type>(ioField, false);    // Read motion data at t_{m,n}
523
524     // Reread field points coordinates for unstructured
525     if (inputType == "unstructured")
```

# checkTable()

From timeVaryingMotionInterpolationPointPatchField.C

```
523
524     // Reread field points coordinates for unstructured
525     if (inputType_ == "unstructured")
526     {
527         // Reread mask data
528         const fileName pointsFile
529         (
530             time.path()
531             /time.caseConstant()
532             /"boundaryData"
533             /inputFolderName_
534             /sampleTimes_[startSampleTime_].name()
535             /"points"
536         );
537         IOobject ioPoints
538         (
539             pointsFile,          // absolute path
540             time,
541             IOobject::MUST_READ,
542             IOobject::NO_WRITE,
543             false,              // no need to register
544             true                 // is global object (currently not used)
545         );
546         startSamplePoints_ = rawIOField<point>(ioPoints, false);    // Read motion points at t_{m,n}
547
548         if (startSampleData_.size() != startSamplePoints_.size())
```

# checkTable()

From timeVaryingMotionInterpolationPointPatchField.C

```
571     }
572 }
573
574 // Update END sampled data fields.
575 if (hi != endSampleTime_)
576 {
577     endSampleTime_ = hi;
578
579     if (endSampleTime_ == -1)
580     {
581         // endTime no longer valid. Might as well clear endValues.
582         if (debug)
583         {
584             Pout<< "checkTable : Clearing endValues" << endl;
585         }
586         endSampledValues_.clear();           // Clear values if current time> t_{m,end}
587         endSampleData_.clear();
588         if (inputType_ == "unstructured")
589         {
590             endSamplePoints_.clear();
591         }
592     }
593     else
594     {
595         if (debug)
596         {
```

# checkTable()

From timeVaryingMotionInterpolationPointPatchField.C

```
674     }
675 }
676
677 // Do the interpolation of the data to mesh coordinates
678 scalar deltaTime = time.value() - sampleTimes_[startSampleTime_].value();
679 bool interpolateEnd = (endSampleTime_ != -1 && deltaTime > SMALL);
680
681 if (interpolationType_ == "trilinear")
682 {
683     applyTrilinearInterpolation
684     (
685         meshPts,
686         interpolateEnd
687     );
688 }
689 else if (interpolationType_ == "nearest")
690 {
691     applyNearestValues
692     (
693         meshPts,
694         interpolateEnd
695     );
696 }
697 else if (interpolationType_ == "inverseDist")
698 {
699     applyInverseDistanceInterpolation
```

# checkTable()

From timeVaryingMotionInterpolationPointPatchField.C

```
687         );
688     }
689     else if (interpolationType_ == "nearest")
690     {
691         applyNearestValues
692         (
693             meshPts,
694             interpolateEnd
695         );
696     }
697     else if (interpolationType_ == "inverseDist")
698     {
699         applyInverseDistanceInterpolation
700         (
701             meshPts,
702             interpolateEnd
703         );
704     }
705     else
706     {
707         FatalErrorInFunction
708             << "Illegal interpolation option."
709             << abort(FatalError);
710     }
711 }
```

# TYPES OF INTERPOLATION:

## NEAREST VALUE:

Direct assignment of the value at the closest data point to the boundary points.

May lead to poor quality results in cases with a coarse point cloud.

Useful when the motion information is provided as a point cloud with sufficient density, so that interpolation between multiple data points does not alter the results significantly.

Hypothetical ideal case: one data point for each mesh boundary point.

Recommendation: use a point cloud with spacing similar to the mesh.



# TYPES OF INTERPOLATION:

## NEAREST VALUE:

```
1165 template<class Type>
1166 void Foam::timeVaryingMotionInterpolationPointPatchField<Type>::applyNearestValues
1167 (
1168     const pointField& meshPts,
1169     const bool& interpolateEnd
1170 )
1171 {
1172     // Create a generic interpolator pointer
1173     autoPtr<pointToPointPlanarInterpolation> interpPtr;
1174
1175     // Always interpolate start values
1176     interpPtr.reset
1177     (
1178         new pointToPointPlanarInterpolation
1179         (
1180             startSamplePoints_, // sourcePoints
1181             meshPts,           // destPoints
1182             0,                 // perturb (not used)
1183             true                // nearestOnly
1184         )
1185     );
1186     startSampledValues_ = interpPtr().interpolate(startSampleData_);
1187
```

# TYPES OF INTERPOLATION:

## NEAREST VALUE:

```
1185     );
1186     startSampledValues_ = interpPtr().interpolate(startSampleData_);
1187
1188     // Interpolate end
1189     if (interpolateEnd)
1190     {
1191         if (inputType_ == "unstructured")
1192         {
1193             interpPtr.reset
1194             (
1195                 new pointToPointPlanarInterpolation
1196                 (
1197                     endSamplePoints_, // sourcePoints
1198                     meshPts,          // destPoints
1199                     0,                // perturb (not used)
1200                     true              // nearestOnly
1201                 )
1202             );
1203         }
1204
1205         endSampledValues_ = interpPtr().interpolate(endSampleData_);
1206     }
1207 }
```

# TYPES OF INTERPOLATION:

## INVERSE DISTANCE:

Follows method described by Shepard with a distance criterion: [3]

$$V_p = \begin{cases} \frac{\sum_{i=1}^n w_i V_i}{\sum_{i=1}^n w_i} & , \text{ for all } i \text{ where } \text{dist}(\mathbf{X}_p, \mathbf{X}_i) \leq R_{\min} , \\ V_i & , \text{ for any } i \text{ where } \text{dist}(\mathbf{X}_p, \mathbf{X}_i) = 0 . \end{cases}$$

$V_i$  is the field value at each used data point  $i$  and  $w_i$  is the corresponding weight factor

$$w_i = \left( \frac{1}{\text{dist}(\mathbf{X}_p, \mathbf{X}_i)} \right)^p ,$$

# TYPES OF INTERPOLATION:

## INVERSE DISTANCE:

```
1  template<class Type> 1210
2  Foam::tmp<Foam::Field<Type>> Foam::timeVaryingMotionInterpolationPointPatchField<Type>::inverseDistance
3  (
4      const pointField& meshPts,
5      const pointField samplePoints,
6      const Field<Type> sampleData
7  ) const
8  {
9      tmp<Field<Type>> tfld(new Field<Type>(meshPts.size()));
10     Field<Type>& fld = tfld.ref();
11
12     // A sortable list for distances from mesh to point data
13     SortableList<scalar> distSorted(samplePoints.size());
14
15     forAll(meshPts, pp) // Iterate through boundary points
16     {
17         // Assign new values to SortableList and sort it
18         distSorted = mag(meshPts[pp]-samplePoints);
19         distSorted.sort();
20
21         Type interpNum(Zero);
22         scalar interpDen(Zero);
23
```

# TYPES OF INTERPOLATION:

## INVERSE DISTANCE:

```
11
12 // A sortable list for distances from mesh to point data
13 SortableList<scalar> distSorted(samplePoints.size());
14
15 forAll(meshPts, pp) // Iterate through boundary points
16 {
17     // Assign new values to SortableList and sort it
18     distSorted = mag(meshPts[pp]-samplePoints);
19     distSorted.sort();
20
21     Type interpNum(Zero);
22     scalar interpDen(Zero);
23
24     forAll(distSorted, jj) // Iterate through distances (ascending)
25     {
26         scalar pointD = distSorted[jj];
27         if (pointD>inverseDistRadius_) // Stop loop if distance > inverseDistRadius_
28         {
29             break;
30         }
31
32         label pointI = distSorted.indices()[jj];
33         if (pointD < SMALL) // dist=0 condition
34         {
```

# TYPES OF INTERPOLATION:

## INVERSE DISTANCE:

```
27         if (pointD>inverseDistRadius_)           // Stop loop if distance > inverseDistRadius_  
28         {  
29             break;  
30         }  
31  
32         label pointI = distSorted.indices()[jj];  
33         if (pointD < SMALL)                         // dist=0 condition  
34         {  
35             interpNum = sampleData[pointI];  
36             interpDen = 1.0;  
37             break;  
38         }  
39  
40         scalar pointInvD = 1/(pointD);              // Inv. dist weight (w_i)  
41  
42         interpNum += pointInvD * sampleData[pointI]; // w_i * V_i  
43         interpDen += pointInvD;  
44     }  
45  
46     if ( interpDen == 0)  
47     {  
48         fld[pp] = Type(Zero);                      // No division by 0  
49     }
```

# TYPES OF INTERPOLATION:

## INVERSE DISTANCE:

```
35         interpNum = sampleData[pointI];
36         interpDen = 1.0;
37         break;
38     }
39
40     scalar pointInvD = 1/(pointD);           // Inv. dist weight (w_i)
41
42     interpNum += pointInvD * sampleData[pointI]; // w_i * V_i
43     interpDen += pointInvD;
44 }
45
46 if ( interpDen == 0)
47 {
48     fld[pp] = Type(Zero);           // No division by 0
49 }
50 else
51 {
52     fld[pp] = interpNum/interpDen;   // Final value at point
53 }
54 }
55
56 return tfld;           // Return field
57 }
```

# TYPES OF INTERPOLATION:

## TRILINEAR INTERPOLATION:

A series of 7 linear interpolations in a regular lattice, using the 8 nearest data vertices to a mesh point.

$$V_{00} = V_{000} (1 - l_x) + V_{100} l_x ,$$

$$V_{10} = V_{010} (1 - l_x) + V_{110} l_x ,$$

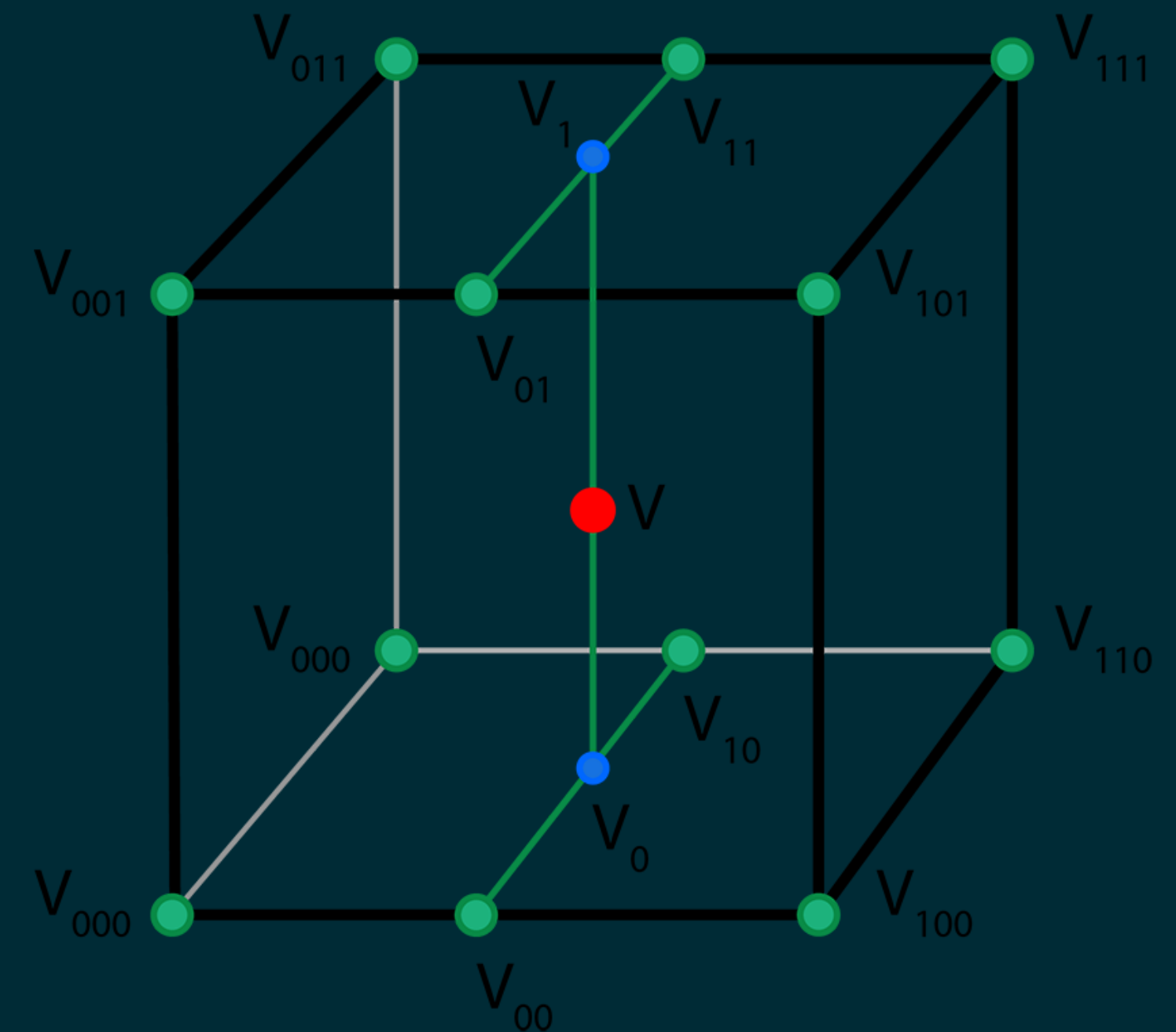
$$V_{01} = V_{001} (1 - l_x) + V_{101} l_x ,$$

$$V_{11} = V_{011} (1 - l_x) + V_{111} l_x ,$$

$$V_0 = V_{00} (1 - l_y) + V_{10} l_y ,$$

$$V_1 = V_{01} (1 - l_y) + V_{11} l_y ,$$

$$V = V_0 (1 - l_z) + V_1 l_z .$$





# TYPES OF INTERPOLATION:

## TRILINEAR INTERPOLATION:

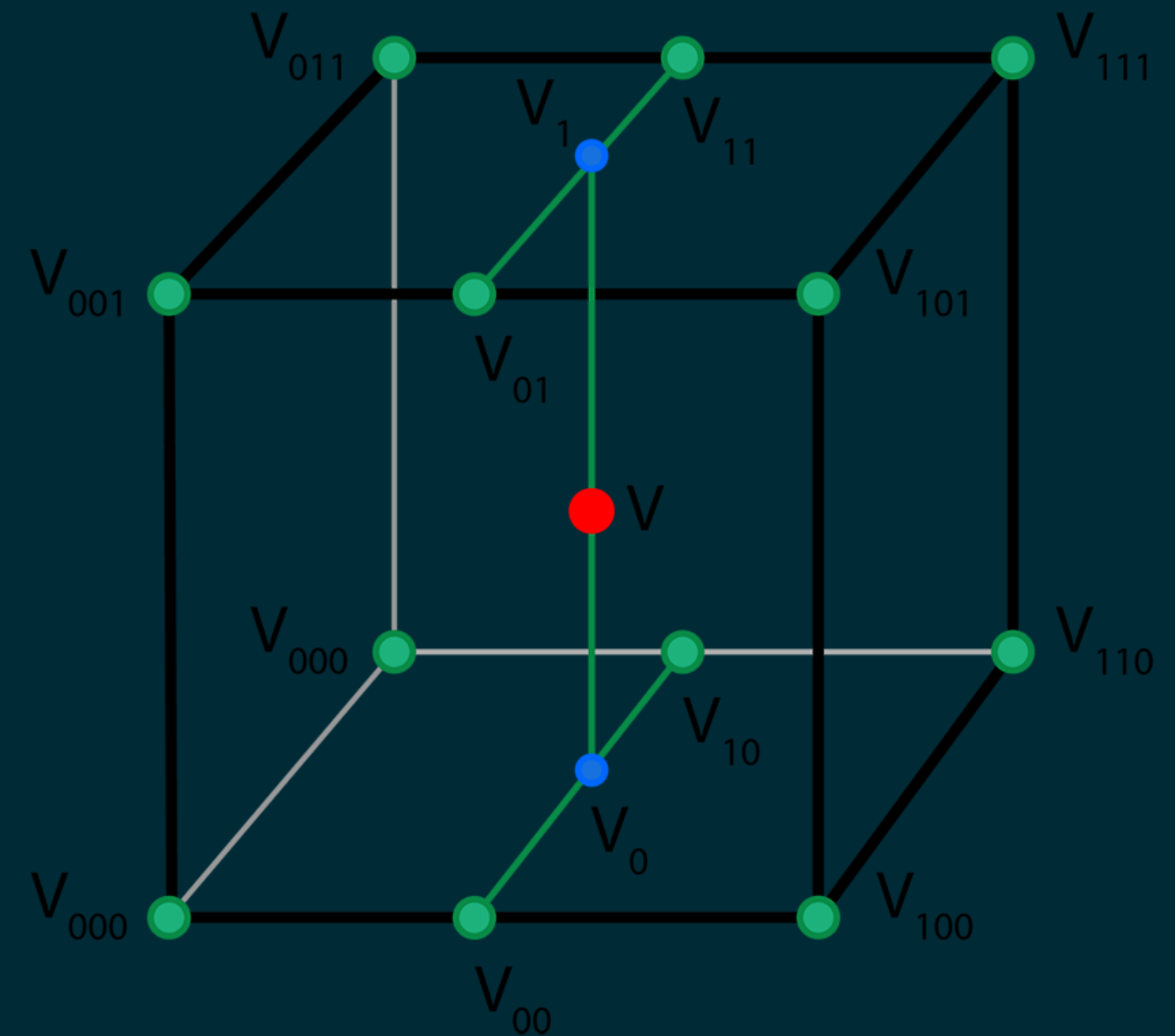
Interpolation factors  $l_x$ ,  $l_y$  and  $l_z$  represent normalised terms for the linear interpolations ranging from 0 to 1 and calculated as

$$l_x = \frac{x_p - x_0}{x_1 - x_0},$$

$$l_y = \frac{y_p - y_0}{y_1 - y_0},$$

$$l_z = \frac{z_p - z_0}{z_1 - z_0},$$

where  $(x_0, y_0, z_0)$  and  $(x_1, y_1, z_1)$  represent the coordinates of points 000 and 111 in the interpolation lattice, and  $(x_p, y_p, z_p)$  represents the point at which data will be interpolated.



# TYPES OF INTERPOLATION:

## LINEAR INTERPOLATION:

Given a linear interpolation factor  $l_f$ , interpolate between two values.

```
714 template<class Type>
715 Type Foam::timeVaryingMotionInterpolationPointPatchField<Type>::linearInterpolation
716 (
717     const Type& edgeVal0,
718     const Type& edgeVal1,
719     const scalar& lf
720 )
721 {
722     return edgeVal0*(1-lf)+edgeVal1*lf;
723 }
```

# TYPES OF INTERPOLATION:

## BILINEAR INTERPOLATION:

Given two linear interpolation factors  $l_{f,1}$  and  $l_{f,2}$ , interpolate between 4 values, in two dimensions.

```
726 template<class Type>
727 Type Foam::timeVaryingMotionInterpolationPointPatchField<Type>::bilinearInterpolation
728 (
729     const Type& edgeVal00,
730     const Type& edgeVal10,
731     const Type& edgeVal01,
732     const Type& edgeVal11,
733     const scalar& lf1,
734     const scalar& lf2
735 )
736 {
737     Type linA = linearInterpolation(edgeVal00,edgeVal10,lf1);
738     Type linB = linearInterpolation(edgeVal01,edgeVal11,lf1);
739     return linearInterpolation(linA,linB,lf2);
740 }
```

# TYPES OF INTERPOLATION:

## TRILINEAR INTERPOLATION:

Given three linear interpolation factors  $l_{f,1}$ ,  $l_{f,2}$  and  $l_{f,3}$ , perform two bilinear interpolations in axes 1 and 2 and a linear interpolation in axis 3.

```
743 template<class Type>
744 Type Foam::timeVaryingMotionInterpolationPointPatchField<Type>::trilinearInterpolation
745 (
746     const Type& edgeVal000,
747     const Type& edgeVal100,
748     const Type& edgeVal010,
749     const Type& edgeVal110,
750     const Type& edgeVal001,
751     const Type& edgeVal101,
752     const Type& edgeVal011,
753     const Type& edgeVal111,
754     const scalar& lf1,
755     const scalar& lf2,
756     const scalar& lf3
757 )
758 {
759     // First bilinear interpolation
```

# TYPES OF INTERPOLATION:

## TRILINEAR INTERPOLATION:

Given three linear interpolation factors  $l_{f,1}$ ,  $l_{f,2}$  and  $l_{f,3}$ , perform two bilinear interpolations in axes 1 and 2 and a linear interpolation in axis 3.

```
755     const scalar& lf2,  
756     const scalar& lf3  
757 )  
758 {  
759     // First bilinear interpolation  
760     Type biLinA = bilinearInterpolation  
761     (  
762         edgeVal000,  
763         edgeVal100,  
764         edgeVal010,  
765         edgeVal110,  
766         lf1,  
767         lf2  
768     );  
769     // Second bilinear interpolation  
770     Type biLinB = bilinearInterpolation  
771     (  
772         edgeVal000,
```

# TYPES OF INTERPOLATION:

## TRILINEAR INTERPOLATION:

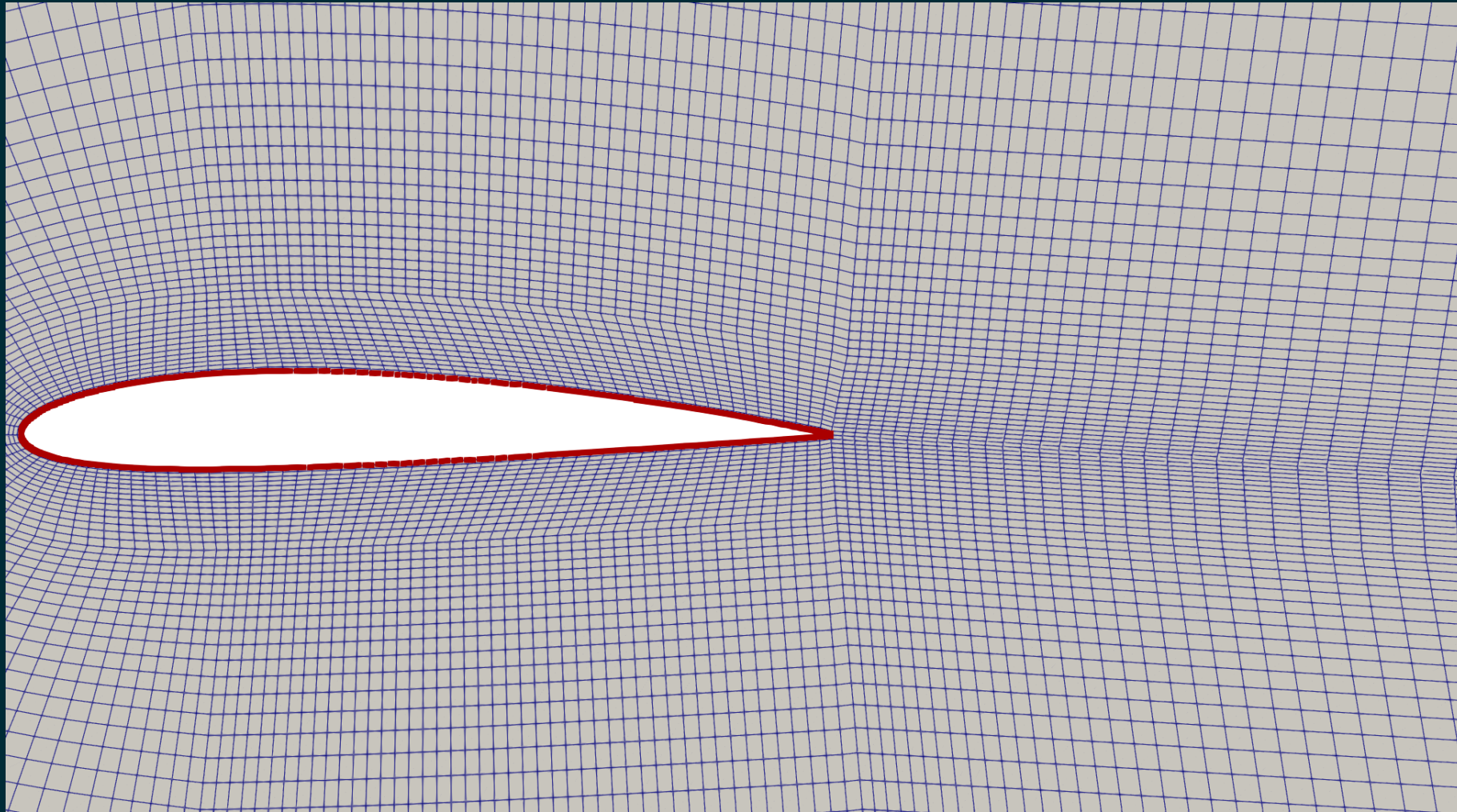
Given three linear interpolation factors  $l_{f,1}$ ,  $l_{f,2}$  and  $l_{f,3}$ , perform two bilinear interpolations in axes 1 and 2 and a linear interpolation in axis 3.

```
765         edgeVal110,  
766         lf1,  
767         lf2  
768     );  
769     // Second bilinear interpolation  
770     Type biLinB = bilinearInterpolation  
771     (  
772         edgeVal000,  
773         edgeVal100,  
774         edgeVal010,  
775         edgeVal110,  
776         lf1,  
777         lf2  
778     );  
779     // Interpolate linearly between the two previous  
780     return linearInterpolation(biLinA,biLinB,lf3);  
781 }
```

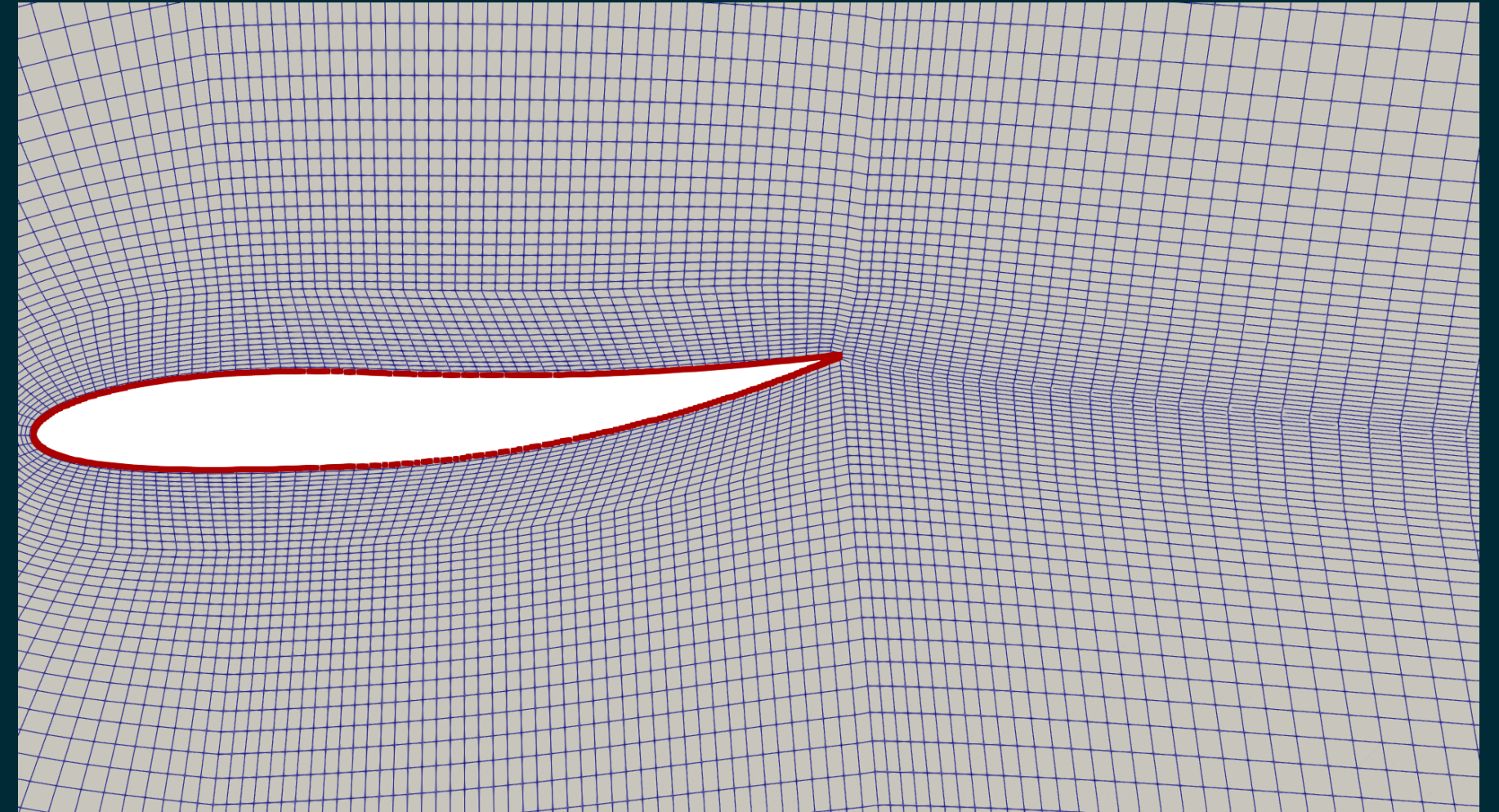


# TUTORIAL 01: DEFORMING 2D AIRFOIL

User-defined NACA 4 digit airfoil. See files in `tutorials/airfoil` and file `tutorials/Allrun_airfoil`.



(a) Initial mesh.



(b) Deformed mesh.

# TUTORIAL 01: DEFORMING 2D AIRFOIL

We will follow `tutorials/Allrun_airfoil`.

Then go through the details of one of the simulation folders.

PRACTICAL SESSION!

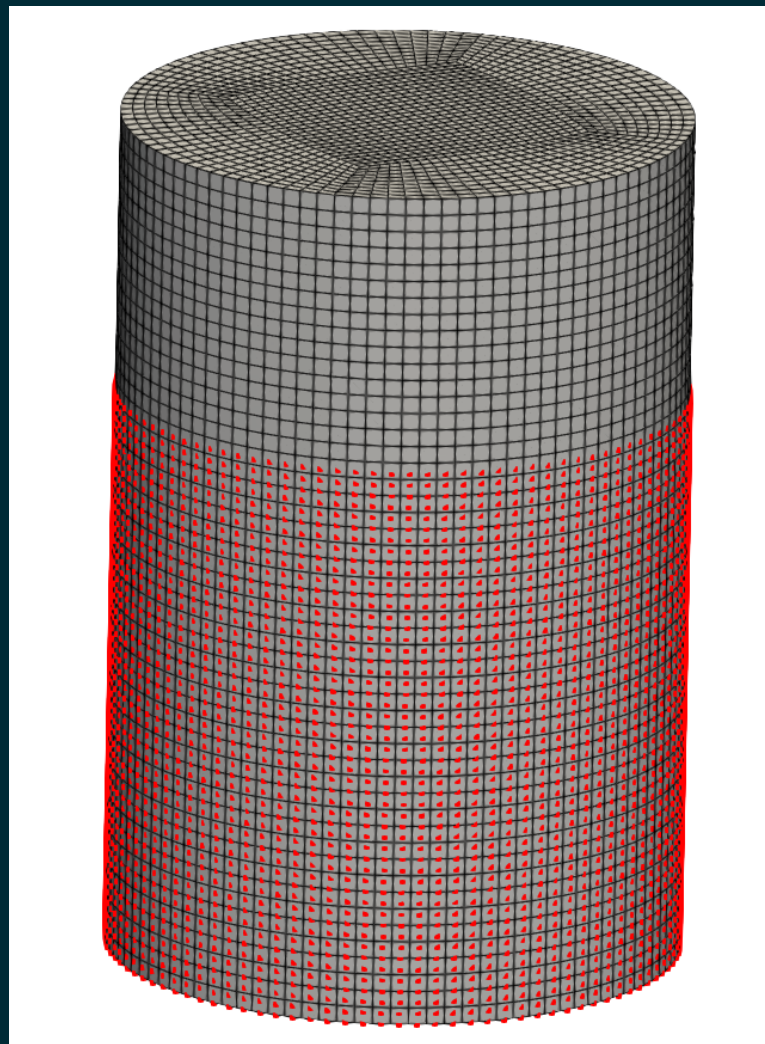
```
1 airfoil
2 |-- 0_orig
3 |   |-- U
4 |   |-- nuTilda
5 |   |-- nut
6 |   |-- p
7 |   |-- pointDisplacement
8 |   |-- pointMotionU
9 |-- Allclean
10 |-- Allrun
11 |-- Allrun_prepare
12 |-- README
13 |-- constant
14 |   |-- dynamicMeshDict
15 |   |-- transportProperties
16 |   |-- turbulenceProperties
17 |-- createNaca4dig.py
18 |-- curiosityFluidsAirfoilMesher.py
19 |-- system
20 |   |-- controlDict
21 |   |-- fvSchemes
22 |   |-- fvSolution
```



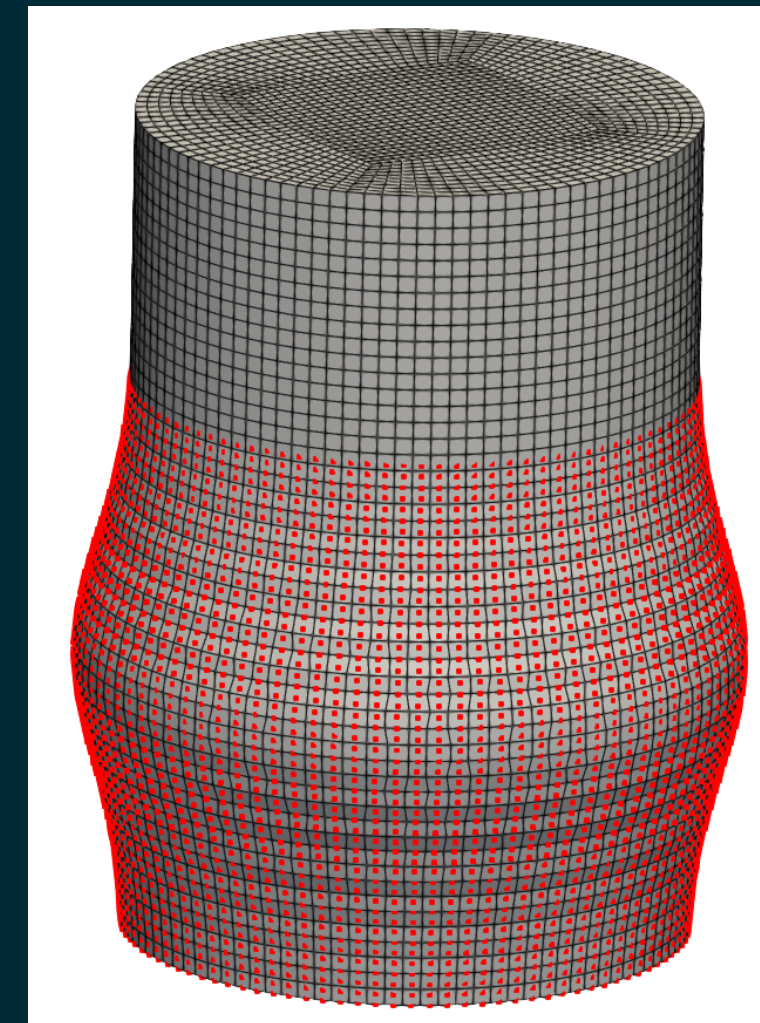
# TUTORIAL 02: DEFORMING 3D CYLINDER

A cylinder with radial deformation as a function of height ( $z$ ) and time.

See files in folder `tutorials/deformingCylinder` and file `tutorials/Allrun_deformingCylinder`.



(a) Initial mesh.



(b) Deformed mesh.

# TUTORIAL 02: DEFORMING 3D CYLINDER

We will follow  
`tutorials/Allrun_deformingCylinder.`

Then go through the details of one of the simulation  
folders.

PRACTICAL SESSION!

```
1  deformingCylinder
2  | -- 0_orig
3  | | -- U
4  | | -- alpha.water
5  | | -- p_rgh
6  | | -- pointDisplacement
7  | | `-- pointMotionU
8  | -- Allclean
9  | -- Allrun
10 | -- Allrun_prepare
11 | -- README
12 | -- constant
13 | | -- dynamicMeshDict
14 | | -- g
15 | | -- transportProperties
16 | | `-- turbulenceProperties
17 | -- createMotion.py
18 | `-- system
19 | | -- blockMeshDict.m4
20 | | -- controlDict
21 | | -- decomposeParDict
22 | | -- fvSchemes
23 | | -- fvSolution
24 | | `-- setFieldsDict
```

# FINAL REMARKS:

`timeVaryingMotionInterpolation` can be improved in many ways:

- `pointToPointPlanarInterpolation` can also be used for 2D Delaunay interpolation (its original purpose).
- Improve non-trilinear interpolation methods for `structured` data, so that a matrix with point coordinates is not needed.
- Allow for structured grids with motion data that are not aligned with global coordinate system.
- Improve temporal interpolation. Linear is not great and can produce motions that not accurately follow the desired motion.

I will have all BC files and tutorials in a [git repository](#) (currently exists, but it is still empty). I hope to add updates/changes in the future.

# THANK YOU!

