Droplet collisions in dieselSpray and implementations of collisions in solidParticle

Developed for OpenFOAM-1.5.dev

Author: Josef Runsten
Peer reviewed by: Anne Koesters Jelena Andric

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Preface

This tutorial is part of the examination of the MSc/PhD course in CFD with OpenSource software, 2010, http://www.tfd.chalmers.se/~hani/kurser/OS_CFD/, at Chalmers University of Technology, Göteborg. The project described in this document is developed and tested in OpenFOAM-1.5-dev and describes a possible way to implement a collision model of solid particles. A thank you to examiner Håkan Nilsson and assistant Jelena Andric for their patience and support during the project.
# Contents

1 Droplet collisions in dieselSpray 3  
1.1 Introduction .................................................... 3  
1.2 Collisions in dieselSpray .................................... 3  
   1.2.1 Selecting collision model ............................... 3  
   1.2.2 The O’Rourke collision model ....................... 3  
   1.2.3 The trajectory collision model ..................... 6  

2 Tutorial: Particle collisions 9  
2.1 Collisions in solidParticle ................................. 9  
   2.1.1 The new solid particle collision model ............. 9  
   2.1.2 Creating collidingSolidParticleFoam .............. 10  
   2.1.3 Detecting collisions .................................. 11  
   2.1.4 Velocity change upon collision ..................... 12  
   2.1.5 Creating the case .................................. 13  
   2.1.6 Running the case .................................. 14  
   2.1.7 Issues and recommendations ....................... 15
Chapter 1

Droplet collisions in dieselSpray

1.1 Introduction
In this chapter the modeling of collisions in the class dieselSpray is described. Today there exist no way to model collisions between solid particles in OpenFOAM-1.5.dev. The aim of the project is to implement such a model in the solidParticle class and to model a collision of two solid particles of equal density and diameter. This could be used as a basic work to create a more advanced collision model.

1.2 Collisions in dieselSpray
In order to implement collision models for solid particles it can be useful to understand how they are used for droplets. Hence, we will have a look at the spray submodels in the class dieselSpray.

1.2.1 Selecting collision model
A case using the dieselSpray class is aachenBomb, located in $FOAM_TUTORIALS/dieselFoam/aachenBomb. In the dictionary constant/sprayProperties the collision model is set to off as default. This can be changed to either ORourke or trajectory, which are two different collision models, found in /$FOAM_SRC/src/lagrangian/dieselSpray/spraySubModels/collisionModel.

1.2.2 The O’Rourke collision model
In the O’Rourke collision model, if a calculated collision probability is high enough and two particles are in the same cell they will collide regardless of their direction. The probability of a collision is the same for parcels heading towards each other as for parcels with opposite directions. The collision frequency increases with smaller cell size, see eq (1.1), but there is no condition saying that two parcels has be close enough that they actually can meet within the time step.

\[
\nu = N_{min} \frac{\pi}{4V_{cell}} (D_{min} + D_{max})^2 |U_{rel}| \Delta t
\]  

(1.1)

where \(N_{min}\) is the number of droplets in the smaller parcel, \(V_{cell}\) is the volume of the cell, \(D\) is the diameter, \(U_{rel}\) is the relative velocity between the droplets and \(\Delta t\) is the time step.
To use this model, make the following changes in /constant/sprayProperties

collisionModel ORourke;//off;
ORourkeCoeffs
{
    coalescence off;
}
Switching coalescence on or off determines if droplets will coalesce after collision or not. If we would like to use this model for solid particles, which can not coalesce, this option would have to be disabled. Let’s have a look at the files associated with the O’Rourke model, located in:

/\$FOAM_SRC/src/lagrangian/dieselSpray/spraySubModels/collisionModel/ORourke/

The O’Rourke collision model class inherits attributes from collisionModel.C, which is an abstract class. We can see this in the beginning of ORourkeCollisionModel.H

class ORourkeCollisionModel :
    public collisionModel
{

In ORourkeCollisionModel.C, the member function ORourkeCollisionModel::collideParcels is used to check if two parcels (a parcel represents a group of droplets with the same physical properties and can be traced as one single droplet. This is used in order to avoid calculating for all droplets, which can be very costly in time) collide. First the size of the spray is checked. If the number of particles is less than 2 there can be no collision.

    if (spray_.size() < 2)
    {
        return;
    }

An iterator is defined that goes through all the parcels in the domain, checks in which cells they are in and if two parcels in an iteration are in the same cell.

    spray::iterator secondParcel = spray_.begin();
    ++secondParcel;
    spray::iterator p1 = secondParcel;

    while (p1 != spray_.end())
    {
        label cell1 = p1().cell();

        spray::iterator p2 = spray_.begin();

        while (p2 != p1)
        {
            label cell2 = p2().cell();

            // No collision if parcels are not in the same cell

            if (cell1 == cell2)
            {
                # include "sameCell.H"
            } // if - parcels in same cell

If that is the case, the file sameCell.H is included, providing the collision behavior of the droplets in the two parcels.

    if (cell1 == cell2)
    {
        # include "sameCell.H"
    } // if - parcels in same cell

The rest of the code in this file deals with removal of the coalesced parcels. The smaller of the two coalesced parcels will be deleted. In sameCell.H the destiny of the parcels in the same cell is decided, based on probabilities depending on cell volume, relative velocity between parcels, size and number of droplets in each parcel. The implementation is the same as described in the KIVA manual [1]. Commented code describing the collision model is shown below.
vector v1 = p1().U(); //Velocity of particle 1
vector v2 = p2().U(); //Velocity of particle 2

vector vRel = v1 - v2; //Relative velocity
scalar magVRel = mag(vRel); //Magnitude of the relative velocity

scalar sumD = p1().d() + p2().d(); //Sum of particle diameters
scalar pc = spray_.p()[p1().cell()]; //Pressure in the cell

//Decided which parcel is smaller
spray::iterator pMin = p1;
spray::iterator pMax = p2;

scalar dMin = pMin().d();
scalar dMax = pMax().d();

if (dMin > dMax) {
    dMin = pMax().d();
    dMax = pMin().d();
    pMin = p2;
    pMax = p1;
}

//Density of the big and small parcel
scalar rhoMax = spray_.fuels().rho(pc, pMax().T(), pMax().X());
scalar rhoMin = spray_.fuels().rho(pc, pMin().T(), pMin().X());

scalar mMax = pMax().m(); //Mass of the big parcel
scalar mMin = pMin().m(); //Mass of the small parcel
scalar mTot = mMax + mMin; //Sum of the two parcel masses

scalar nMax = pMax().N(rhoMax); //Number of droplets in the big parcel
scalar nMin = pMin().N(rhoMin); //Number of droplets in the small parcel
scalar mdMin = mMin/nMin; //Mean mass of droplets in the small parcel

//Calculating the probability of collisions, according to the KIVA manual
scalar nu0 = 0.25*mathematicalConstant::pi*sumD*sumD*magVRel*dt/vols_[cell1];

scalar nu = nMin*nu0; //Collision frequency
scalar collProb = exp(-nu); //Collision probability
scalar xx = rndGen_.scalar01(); //Random number between 0 and 1

// Collision occur
if ((xx > collProb) && (mMin > VSMALL) && (mMax > VSMALL)) {

The intermediate part of the code deals with the probability for coalescence. In this project the focus is not on this. For grazing collisions (no coalescence) the parcel speed and direction after collision depends on the random restitution coefficient $g_f$, and is calculated ensuring conservation of momentum.

// Grazing collision (no coalescence)
else {
    scalar gf = sqrt(prob) - sqrt(coalesceProb); //Restitution coefficient
    scalar denom = 1.0 - sqrt(coalesceProb);
}
if (denom < 1.0e-5) {
    denom = 1.0;
}

gf /= denom; //Not used if coalescence is turned off

// if gf negative, this means that coalescence is turned off
// and these parcels should have coalesced
gf = max(0.0, gf);

//Density of parcel 1 and 2
scalar rho1 = spray_.fuels().rho(pc, p1().T(), p1().X());
scalar rho2 = spray_.fuels().rho(pc, p2().T(), p2().X());

scalar m1 = p1().m();  //Mass of parcel 1
scalar m2 = p2().m();  //Mass of parcel 2
scalar n1 = p1().N(rho1); //Number of droplets in of parcel 1
scalar n2 = p2().N(rho2); //Number of droplets in of parcel 2

//New velocities are calculated using the random restitution coefficient
// gf -> 1 => v1p -> p1().U() ...
// gf -> 0 => v1p -> momentum/(m1+m2)
vector mr = m1*v1 + m2*v2;

//Conservation of momentum is assured
vector v1p = (mr + m2*gf*vRel)/(m1+m2);
vector v2p = (mr - m1*gf*vRel)/(m1+m2);

if (n1 < n2) {
    p1().U() = v1p;
    p2().U() = (n1*v2p + (n2-n1)*v2)/n2;
}
else {
    p1().U() = (n2*v1p + (n1-n2)*v1)/n1;
    p2().U() = v2p;
}

1.2.3 The trajectory collision model

If we instead want to use the trajectory model [2] we specify this in constant/sprayProperties and add the coalescence switch again (set to off even in this case if we want to use it for solid particles). cSpace and sTime are model constants related to spatial and temporal collision probability decay.

```plaintext
collisionModel trajectory;//off;
trajectoryCoeffs
{
    cSpace    1;
    cTime     0.3;
    coalescence off;
}
```

trajectoryModel.C and trajectoryModel.H look the same as the O'Rourke model files. The difference is how the collision is handled once two parcels are in the same cell. This is decided in the header file trajectoryCM.H which is similar to the header file sameCell.H in the O'Rourke collision model. The main difference is that the direction of travel of the parcels is taken into account, see figures 1.1-1.2.
vector \( p = p2().\text{position}() - p1().\text{position}(); \) //Distance vector between parcels
scalar dist = mag(p); //Distance between parcels

//Dot product of vRel and norm. distance vector
scalar vAlign = vRel & (p/(dist+SMALL));

if (vAlign > 0) //Collision ONLY IF the parcels are traveling towards each other
{

![Figure 1.1: Velocity direction does not matter in O'Rourke. Opposite directions have just as high chance of collision as two particles heading towards each other.](image1)

![Figure 1.2: Trajectory model takes direction into account, as well as checks if collision can occur within the current time step.](image2)

The second difference to the O’Rourke model is the consideration if a collision is possible within the current time step, see eq. 1.2. Compared to the O’Rourke model the trajectory model takes care of the position and direction of travel of the parcels. The distance between the parcels must be smaller than the maximal distance defined by the relative velocity between the parcels times the time step.

\[
U_{align} \Delta t > \frac{|x_2 - x_1| - D_{max} + D_{min}}{2} \tag{1.2}
\]

where

\[
U_{align} = U_{rel} \cdot \frac{x_2-x_1}{|x_2-x_1|}
\]

The collision probability is calculated roughly the same way as in O’Rourke, with a few modifications. \( \alpha \) and \( \beta \) are used to ensure that the parcels, when they reach the projected collision point, will be there at the same time.

scalar v1Mag = mag(v1); //Magnitude of velocity of parcel 1
scalar v2Mag = mag(v2); //Magnitude of velocity of parcel 2
vector nv1 = v1/v1Mag; //Normalized velocity of parcel 1
vector nv2 = v2/v2Mag; //Normalized velocity of parcel 2

scalar v1v2 = nv1 & nv2; //Dot product of the normalized velocities

//Dot product of the normalized velocity and distance vector
scalar vip = nv1 & p;
scalar v2p = nv2 & p;

// The probability is calculated using a special condition
scalar det = 1.0 - v1v2*v1v2;

scalar alpha = 1.0e+20;
scalar beta = 1.0e+20;

if (mag(det) > 1.0e-4)
{
    beta = -(v2p - v1v2*v1p)/det;
    alpha = v1p + v1v2*beta;
}

alpha /= v1Mag*dt;
beta /= v2Mag*dt;

// Is collision possible within this time step
if ((alpha>0) && (alpha<1.0) && (beta>0) && (beta<1.0))
{
    vector p1c = p1().position() + alpha*v1*dt; // New parcel position
    vector p2c = p2().position() + beta*v2*dt; // New parcel position

    scalar closestDist = mag(p1c-p2c); // New distance between parcels

    scalar collProb = // Probability of collision
        pow(0.5*sumD/max(0.5*sumD, closestDist), cSpace_)
        *exp(-cTime_*mag(alpha-beta));
Chapter 2

Tutorial: Particle collisions

2.1 Collisions in solidParticle

Currently, there is no collision model implemented in the solidParticle class. In order to introduce such a model, several changes need to be made. Without going into too much detail on how the solidParticle class is built, this section describes the parts needed in order to implement a simple collision model in this class. The O’Rourke and trajectory collision model implemented in the dieselSpray class that were described previously will not be implemented for the collisions of solid particles. Instead a much simpler model of only two identical solid particles will be used. The chosen model is developed for solid particles, which makes more sense than to use a model created for droplets (where phenomena like breakup and coalescence are present). Implementing the entire structure of the collision models in dieselSpray was considered too complex and more suitable for a larger project, hence we will study only two particles.

2.1.1 The new solid particle collision model

The collision model we will use in this project is from ERCOFTAC [3]. It is based on preserving momentum between particles. The model is simplified by saying that the angular velocity of the particles is 0 and that the collisions are non-sliding. The velocities are then reduced to the following expressions.

\[
\begin{align*}
    u_{p1}^* &= u_{p1} + \frac{J_x}{m_{p1}}, & u_{p2}^* &= -\frac{J_x}{m_{p2}} \\
    v_{p1}^* &= v_{p1} + \frac{J_y}{m_{p1}}, & v_{p2}^* &= -\frac{J_y}{m_{p2}} \\
    w_{p1}^* &= +\frac{J_z}{m_{p1}} = 0, & w_{p2}^* &= -\frac{J_z}{m_{p2}} = 0
\end{align*}
\]

where \( * \) denotes the new values and \( J_x, J_y, J_z \) are the components of the impulsive force and reads (again reduced by the assumption of no angular velocity or sliding):

\[
\begin{align*}
    J_x &= -(1 + e)u_{p1} \frac{m_{p1} m_{p2}}{m_{p1} + m_{p2}} \\
    J_y &= -\frac{2}{\sqrt{3}} v_{p1} \frac{m_{p2} m_{p2}}{m_{p1} + m_{p2}} \\
    J_z &= 0
\end{align*}
\]

where \( e \) is the coefficient of restitution. Note that the new velocities for BOTH particles depend only on mass of the particles and the old velocity of the FIRST particle. This will turn out to be an important part of programming the new model.
2.1.2 Creating collidingSolidParticleFoam

Now let us get started with the modifications. First we need to get solidParticleFoam, created by Håkan Nilsson. Do this through subversion:

```bash
cd $FOAM_RUN
svn checkout http://openfoam-extend.svn.sourceforge.net/svnroot/openfoam-extend/trunk/Breeder_1.5/solvers/other/solidParticleFoam/
cd solidParticleFoam/
```

Rename the directory for the new solver and copy the needed solidParticle files into it. Find and replace all occurances of `solidParticle` with `collidingSolidParticle` in all the files and then rename the files.

```bash
mv solidParticleFoam collidingSolidParticleFoam
cd collidingSolidParticleFoam
wclean
cp $FOAM_SRC/lagrangian/solidParticle/solidParticle* .
cp -r $FOAM_SRC/lagrangian/solidParticle/lnInclude .
```

```bash
sed -i s/solidParticle/collidingSolidParticle/g solidParticle.C collidingSolidParticle.C
sed -i s/solidParticle/collidingSolidParticle/g solidParticleCloud.C collidingSolidParticleCloud.C
sed -i s/solidParticle/collidingSolidParticle/g solidParticleCloud.H collidingSolidParticleCloud.H
sed -i s/solidParticle/collidingSolidParticle/g solidParticleFoam.C collidingSolidParticleFoam.C
sed -i s/solidParticle/collidingSolidParticle/g solidParticle.H collidingSolidParticle.H
sed -i s/solidParticle/collidingSolidParticle/g solidParticleI.H collidingSolidParticleI.H
sed -i s/solidParticle/collidingSolidParticle/g solidParticleIO.C collidingSolidParticleIO.C
```

Edit the files Make/arches

```bash
collidingSolidParticleFoam.C
collidingSolidParticle.C
collidingSolidParticleIO.C
collidingSolidParticleCloud.C
```

```bash
EXE = $(FOAM_USER_APPBIN)/collidingSolidParticleFoam
and Make/options
```

```bash
EXE_INC = \\
-1$(LIB_SRC)/finiteVolume/lnInclude \\
-1$(LIB_SRC)/lagrangian/basic/lnInclude
```

```bash
EXE_LIBS = \\
-1finiteVolume \\
-1lagrangian
```

We can now compile the solver and run the supplied case, in order to make sure that everything is working properly. In the solver directory, type

```bash
wmake
cd ../box
blockMesh
collidingSolidParticleFoam >log
```
To post process, type

```
foamToVTK
paraview
```

Load by clicking File>Load State>baseState.pvsm. A box with two moving particles should open up. Notice that no collision occurs using this solver. We can now modify this without affecting the original code.

### 2.1.3 Detecting collisions

The condition used to detect the occurrence of a collision is similar to that of the O’Rourke model in the dieselSpray class in the sense that the particles have to be in the same cell. A second condition is that the distance between the two particles at the current time has to be less or equal to the average particle diameter. This latter condition is a simpler version of the one used in the trajectory model, where a possible collision is checked for the entire duration of the time step. To use this model, changes in collidingSolidParticleCloud.C have to be made. After the member functions, add the following:

```cpp
void Foam::collidingSolidParticleCloud::checkCell()
{
    List<label> lcell((*this).size());
    List<scalar> ld((*this).size());
    List<vector> lU((*this).size());
    List<vector> lposition((*this).size());
    bool collision;

    label i=0;
    forAllConstIter(Cloud<collidingSolidParticle>,*this,iter)
    {
        const collidingSolidParticle& p=iter();
        lcell[i]=p.cell();
        //Info <<"Particle " <<i<< " is in cell "<<lcell[i]<<endl;
        lU[i]=p.U();
        ld[i]=p.d();
        lposition[i]=p.position();
        i++;  
    }

    //Info <<p0-p1 = "<<mag(lposition[0]-lposition[1])<<endl;
    //Info <<"Diameter = "<<(ld[0]+ld[1])/2<<endl;

    //Only works for two particles.
    if (lcell[0]==lcell[1] && mag(lposition[0]-lposition[1])<=(ld[0]+ld[1])/2)
    {
        collision=true;
    }
    else
    {
        collision=false;
    }

    collision_=collision;
}
```
Also, make sure to add `#include "vector.H"` to the list of included files. The above function checks if the two particles are in the same cell. Lists of particle cell, diameter, velocity and position are created and corresponding values are assigned in the following for-loop. In the if-statement we check if the collision requirements are satisfied. At the end we save the velocity of the first particle for the current time step, which will be used to calculate new values after collision. In `collidingSolidParticleCloud.H`, add

```cpp
bool collision_;  
vector U0_; 
```

to the private member data, and

```cpp
void checkCell(); 
bool collision(){return collision_;}; 
inline vector U0(){return U0_;}; 
```
to public member functions.

### 2.1.4 Velocity change upon collision

In the solidParticle class the particles are collected in what is called a cloud, similar to a spray in the dieselSpray class. This cloud, here declared as `particles` is of the collidingSolidParticleCloud class. In order to get the particles in the cloud to move, we have the member function `Foam::collidingSolidParticleCloud::move(const dimensionedVector& g)`. This function, in turn, uses another `move` function located in the `collidingSolidParticle` class. This is where the velocity of the particle is changed, and here the expressions for the new velocity after a collision will be inserted. We need to add a substantial piece of code. In `collidingSolidParticle.C` replace

```cpp
U_ = (U_ + dt*(Dc*Uc + (1.0 - rhoc/rhop)*td.g()))/(1.0 + dt*Dc);
```

with

```cpp
scalar e = td.spc().e(); //Restitution coefficient  
scalar m = rhop*d_*d_*d_*mathematicalConstant::pi*4.0/3.0; //Particle mass  
bool checkcoll=td.spc().collision();  
//if(checkcoll){Info<<"Particles collide!"<<endl;}  
vector V0=td.spc().U0(); //OLD velocity of particle 1 
scalar Jx = -(1.0+e)*V0.x()*m*m/(2.0*m); //Impulsive force x-comp  
scalar Jy = -2.0/7.0*V0.y()*m*m/(2.0*m); //Impulsive force y-comp  

if(ID_==0 && checkcoll) //Collision for particle 1  
{
    U_.x()=V0.x()+Jx/m;  
    U_.y()=V0.y()+Jy/m;  
    U_.z()=0.0;  
}  
if(ID_==1 && checkcoll) //Collision for particle 2  
{
    U_.x() = -Jx/m;  
    U_.y() = -Jy/m;  
    U_.z() = 0.0;  
}
```

12
//If no collision
U_ = (U_ + dt*(Dc*Uc + (1.0 - rhoc/rhop)*td.g()))/(1.0 + dt*Dc);

The restitution coefficient is defined, particle mass is computed from density and diameter, occurrence of collision is checked and the velocity for the first particle is assigned variable V0. In the next section we calculate the new velocities for the particles. This is why we need V0. The ID_ variable is used to distinguish between the two particles and is specified in a dictionary in the 0 directory of the case (see section 2.1.5). This is a rather complex way of keeping track of both particles, but was found to be necessary. If/when expanding the code to apply for more general cases with large amounts of particles, this needs to be taken care of. In addition to the changes in the .C file, we also need some additional lines in collidingSolidParticle.H and collidingSolidParticleIO.C. Add

```cpp
// Particle ID
scalar ID_;
```

after vector U_; in the private member data in collidingSolidParticle.H.

In collidingSolidParticleIO.C add

```cpp
IOField<scalar> ID(c.fieldIOobject("ID"));
c.checkFieldIOobject(c, ID);
```

after c.checkFieldIOobject(c, d); and

```cpp
p.ID_ = ID[i];
```

after p.U_ = U[i]; in the readFields function.

Similarly, add

```cpp
IOField<scalar> ID(c.fieldIOobject("ID"), np);
```

after IOField<vector> U(c.fieldIOobject("U"), np); and

```
ID[i] = p.ID_;
```

after U[i] = p.U_; and

```
ID.write();
```

after U.write(); in the writeFields function.

The last step is to call the checkcell function from collidingSolidParticleFoam.C. Before particles.move(g); add

```cpp
particles.checkCell();
```

Compile again by typing wmake. Now you should have a working solver collidingSolidParticleFoam. It is now time to set up a case and make some particles collide.

### 2.1.5 Creating the case

We will make some changes to the box case supplied. First change the mesh parameters. In constant/polyMesh/blockMeshDict change the blocking to

```
hex (0 1 2 3 4 5 6 7) (3 3 3) simpleGrading (1 1 1)
```

Run blockMesh to get a new mesh. In 0/lagrangian/defaultCloud/ we have files for particle diameter as well as particle initial positions and velocities. We need to add a file for particle IDs. Copy the diameter file
2.1. COLLISIONS IN SOLIDPARTICLE CHAPTER 2. TUTORIAL: PARTICLE COLLISIONS

```
cp d ID
and change it’s context to

FoamFile
{
   version 2.0;
   format ascii;
   class scalarField;
   location "0";
   object ID;
}

// ************************************************************************* //
```

In the U file, change the velocities to \(2((1.0 \ 0 \ 0) \ (-1.0 \ 0 \ 0))\). In positions, set the coordinates to

\[2((1e-2 \ 9e-2 \ 0.05) \ 15 \ (7e-2 \ 9e-2 \ 0.05) \ 16)\]

What is set is the \(x\), \(y\) and \(z\) coordinate of the two particles, as well as specifying which cell they are in (in this case 72). The values above can of course be set to whatever you want, but this will show a nice collision.

2.1.6 Running the case

While in the box directory, run the case by typing

```
collidingSolidParticleFoam >log
```

To post process, type

```
foamToVTK
paraview
```

Load by clicking File>Load State>baseState.pvsm. The particle ID, described in section 2.1.4, is helpful in post-processing. In the Display tab for Glyph1 choose to color the glyphs by ID, see Figure 2.1. This will let us distinguish between the two particles. Change the glyph type to Cone in order to see the direction of the particles. Hitting the play button will start the animation of the two particles.
2.1.7 Issues and recommendations

Examining the collision closely in paraview, it can be seen that the colliding particles change their position before the new velocities have an effect, see figure 2.2. The velocities are calculated according to the collision model, but the new positions of the particles are calculated using previous values. In the figure it is shown that in the time step after the collision occurs, the direction of the cones are in the direction of the new velocity vectors, but in the wrong coordinates. In the following time step, however, the particles follow the correct path. As a consequence of this error, it is possible for two particles that have recently collided, to do so again in the next few time steps (almost happens in the third step after collision in figure 2.2), which would not be possible if the velocity change was instantaneous. For a more accurate model this needs to be sorted out. As mentioned before, the solver applied in this tutorial only works for two particles. If a greater number of particles is desired, the way of hard coding all particle parameters is not sustainable. The collision check used in collidingSolidParticleCloud.C needs to be looped for all particles instead of comparing only two. In collidingSolidParticle.C the velocities are computed depending on the particle ID. A more general code for this needs to be written, since now we only check if the ID is 0 or 1. Something similar to the structure of the collision models in dieselSpray should be possible. The collision model
applied in this tutorial requires the time step to be small, since collision conditions are checked only for the exact time step values and not for the duration of the time step, as in the trajectory model. This could be taken care of by implementing a similar expression.
Bibliography

